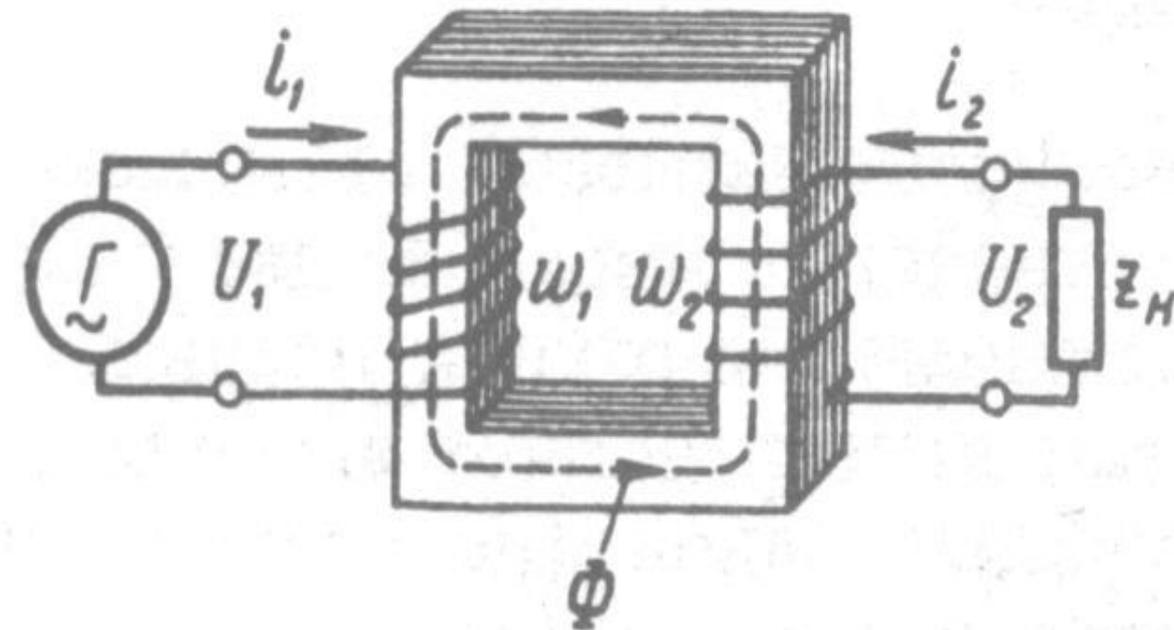


Трансформаторы

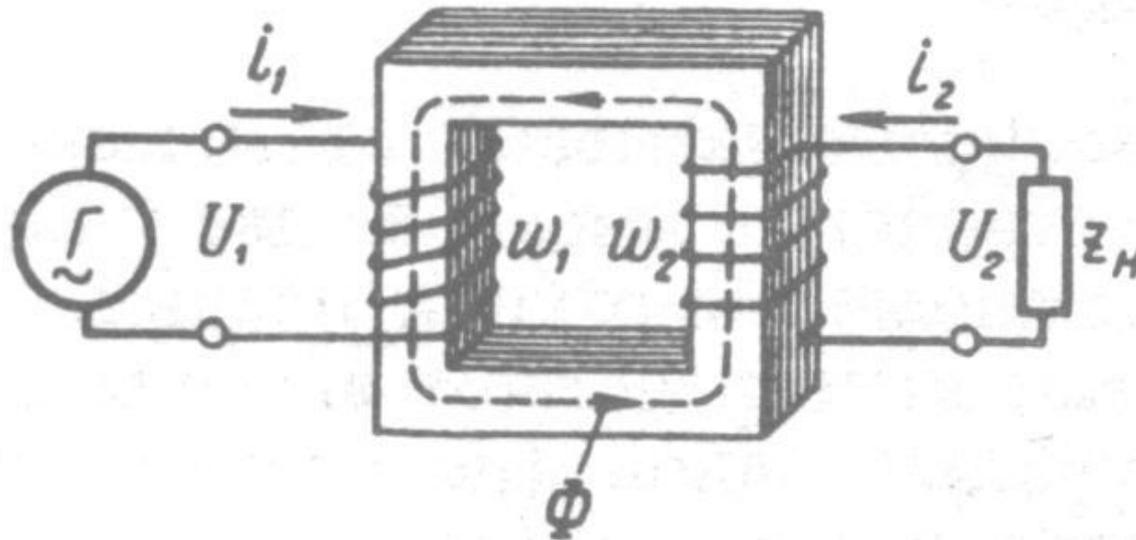
Трансформатор – статическое электромагнитное устройство, имеющее две (или более) индуктивно связанные обмотки, и предназначенное для преобразования посредством явления электромагнитной индукции одной (первичной) системы переменного тока в другую (вторичную) систему переменного тока.



$$e_1 = -w_1 \frac{d\Phi}{dt}$$

$$e_2 = -w_2 \frac{d\Phi}{dt}$$

Идеализированный трансформатор



Режим холостого

хода
 $\frac{d\Phi}{dt}$

$$e_1 = -w_1 \frac{d\Phi}{dt}$$

$$e_2 = -w_2 \frac{d\Phi}{dt}$$

$$U_1 = i_1 r_1 + w_1 \frac{d\Phi}{dt}$$

$$\Phi = \Phi_M \sin \omega t$$

$$\omega = 2\pi f$$

$$U_1 = i_1 r_1 - e_1$$

$$U_1 + e_1 = 0$$

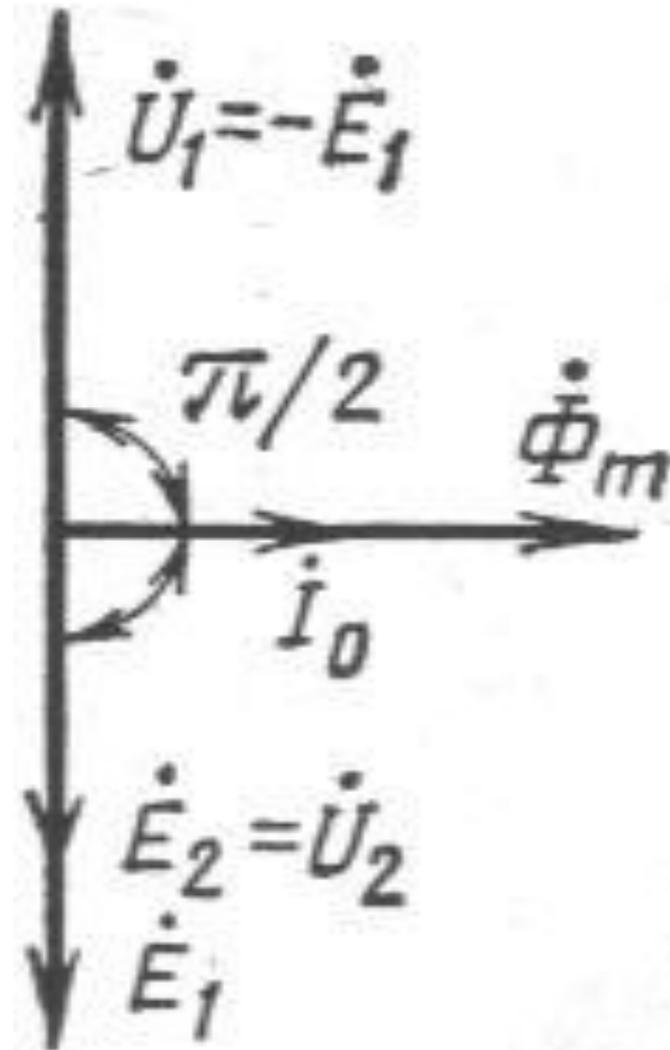
$$e_1 = -\omega \cdot w_1 \Phi_M \cdot \cos \omega t = 2\pi f w_1 \Phi_M \sin \left(\omega t - \frac{\pi}{2} \right)$$

$$e_2 = -\omega \cdot w_2 \Phi_M \cdot \cos \omega t = 2\pi f w_2 \Phi_M \sin \left(\omega t - \frac{\pi}{2} \right)$$

$$\left[\begin{array}{l} E_1 = \frac{2\pi}{\sqrt{2}} f w_1 \Phi_M = 4,44 f w_1 \Phi_M \\ E_2 = \frac{2\pi}{\sqrt{2}} f w_2 \Phi_M = 4,44 f w_2 \Phi_M \end{array} \right]$$

$$\frac{E_1}{E_2} = \frac{w_1}{w_2} \quad \frac{U_1}{U_2} \approx \frac{E_1}{E_2} = \frac{w_1}{w_2} = k$$

$$\dot{U} + \dot{E} = 0$$



Режим

нагрузки

$$U_1 = w_1 \frac{d\Phi_1}{dt} + w_1 \frac{d\Phi_2}{dt} = w_1 \frac{d}{dt} (\Phi_1 + \Phi_2)$$

$$e_1 = -w_1 \frac{d}{dt} (\Phi_1 + \Phi_2)$$

$$U_1 + e_1 = 0$$

$$\Phi_1 + \Phi_2 = \Phi_0$$

$$\dot{\Phi}_{M1} + \dot{\Phi}_{M2} = \dot{\Phi}_{M0}$$

Магнитодвижущая сила (МДС) – намагничивающая сила – характеристика способности источников магнитного поля (эл. токов) создавать магнитные потоки.

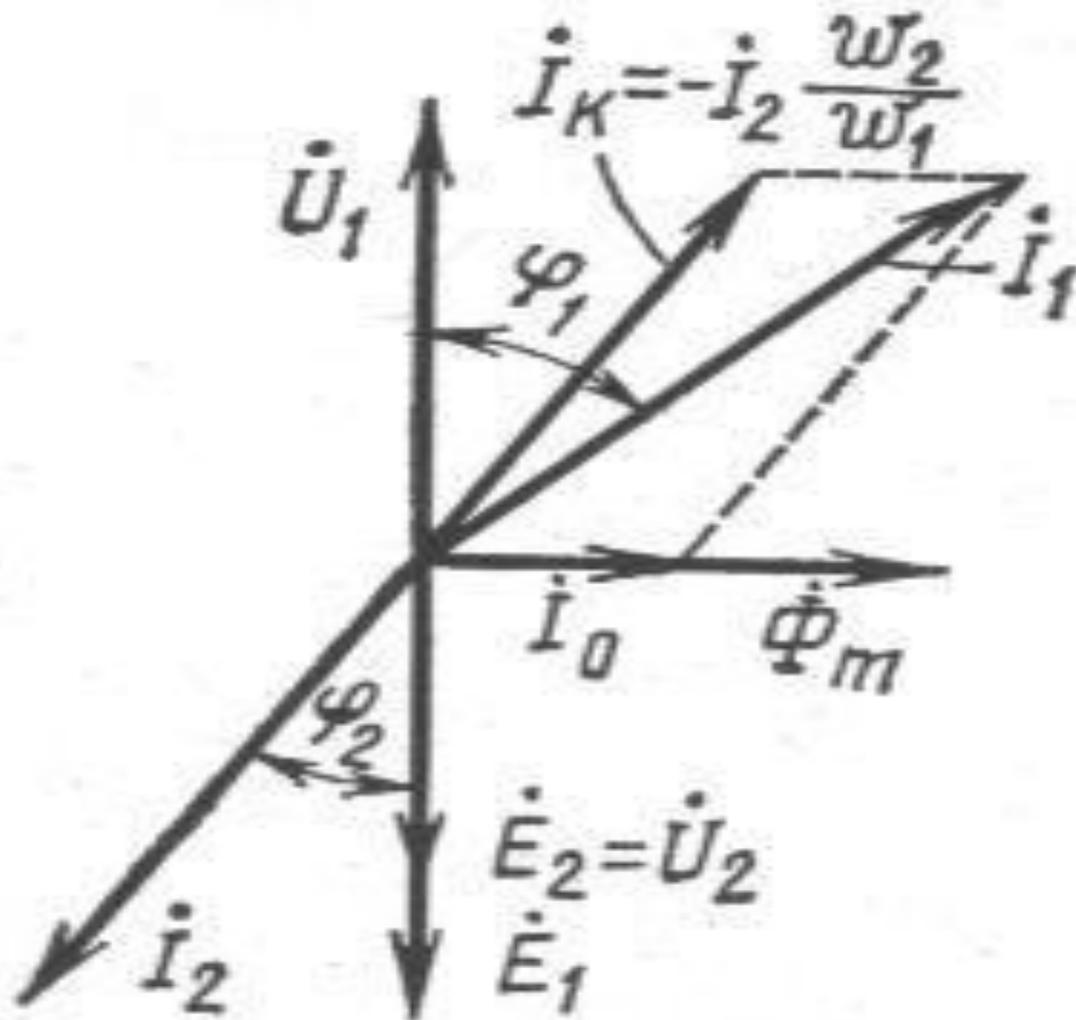
$$\dot{F}_1 + \dot{F}_2 = \dot{F}_0$$

$$\sqrt{2} \dot{I}_1 w_1 + \sqrt{2} \dot{I}_2 w_2 = \sqrt{2} \dot{I}_0 w_1 \quad | \quad \sqrt{2} w_1$$

$$\dot{I}_1 = \dot{I}_0 + \left[-\dot{I}_2 \left(\frac{w_2}{w_1} \right) \right] \quad \dot{I}_K = -\dot{I}_2 \left(\frac{w_2}{w_1} \right)$$

$$\dot{I}_1 = \dot{I}_0 + \dot{I}_K$$

$$I_K E_1 \cos \varphi_2 = I_2 \left(\frac{w_2}{w_1} \right) E_2 \left(\frac{w_1}{w_2} \right) \cos \varphi_2 = I_2 E_2 \cos \varphi_2$$



$$\Phi = \Phi_M \sin \omega t$$

$$\Phi_M = \frac{E_1}{4,44 f w_1}$$

Намагничивающий ток и ток холостого хода

Магнитная характеристика трансформатора, как и других машин переменного тока, дает связь между амплитудными или мгновенными значениями потока и МДС.

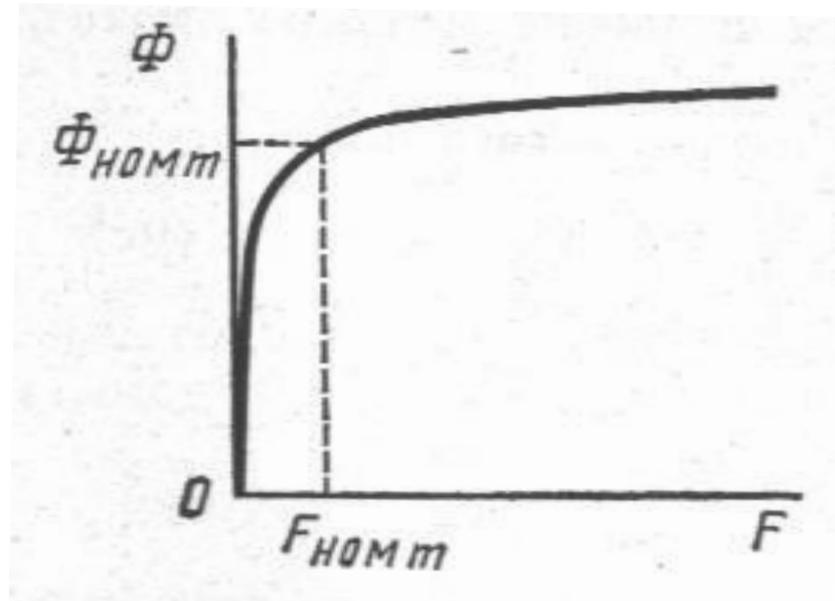
$$F = F_{\text{СТ}} + F_{\text{Я}} + F_{\text{З}}$$

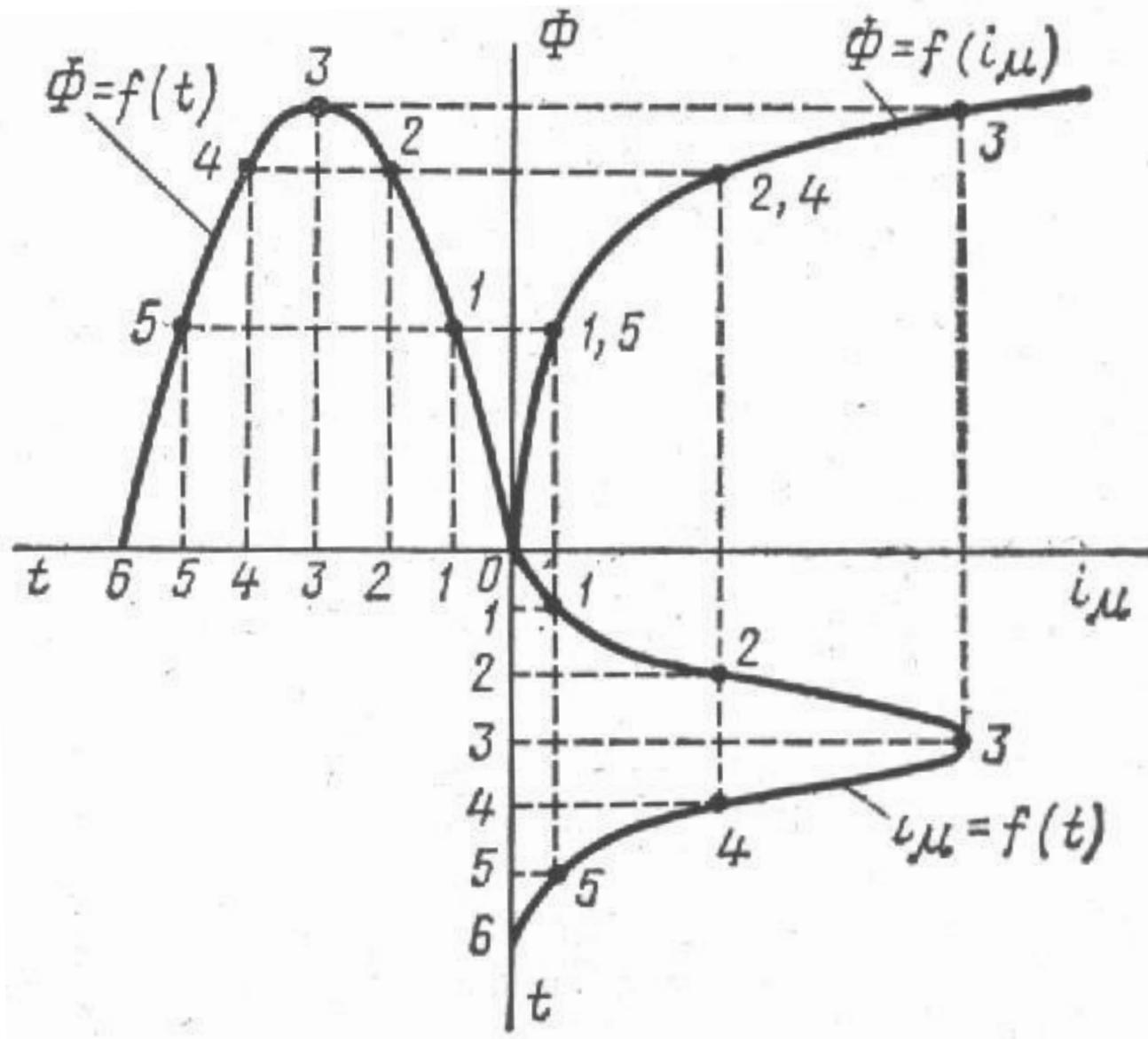
$$\Phi = f(F)$$

$$F_{\text{СТ}} = H_{\text{СТ}} I_{\text{СТ}}$$

$$F_{\text{Я}} = H_{\text{Я}} I_{\text{Я}}$$

$$F_{\text{З}} = H_{\text{З}} I_{\text{З}}$$





$$i_\mu = \frac{F}{w_1}$$

$$I_{\mu} = \sqrt{I_{\mu 1}^2 + I_{\mu 3}^2 + I_{\mu 5}^2 + I_{\mu 7}^2 + \dots}$$

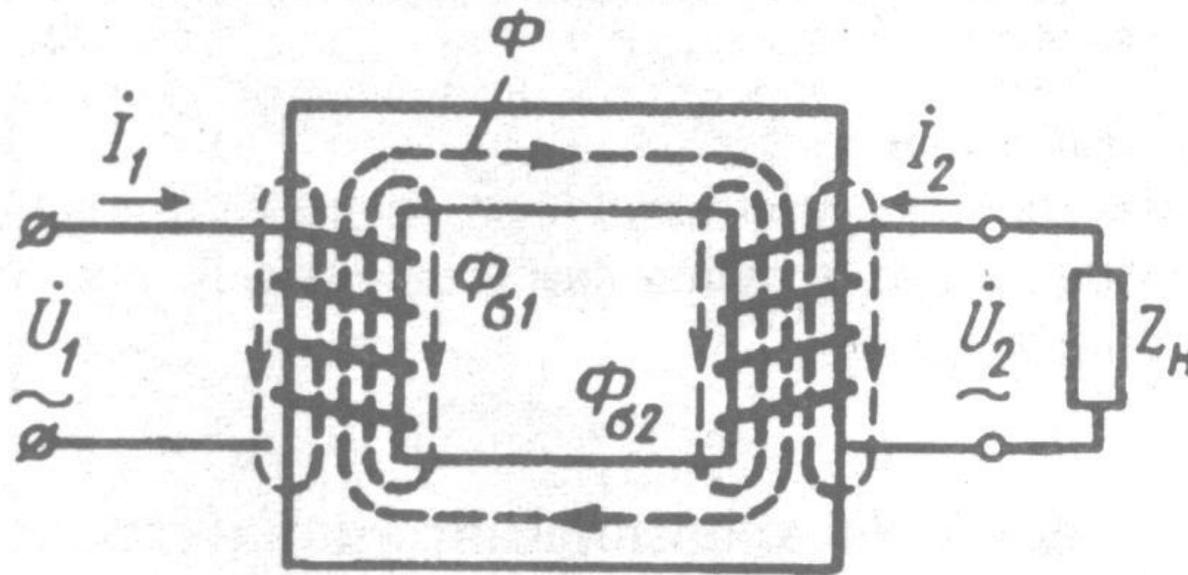
$$I_{\mu} = I_{\mu 1} \sqrt{1 + \alpha^2 + \beta^2 + \gamma^2 + \dots} = k_D I_{\mu 1}$$

$$I_{\mu} = I_{OP} \quad I_{\mu} \approx I_{\mu 1} \quad I_{oa} = \frac{\Delta P_M}{U_1}$$

$$\dot{I}_o = \dot{I}_{\mu} + \dot{I}_{ao}$$

$$I_o = \sqrt{I_{\mu}^2 + I_{ao}^2}$$

Комплексные уравнения и векторные диаграммы трансформатора



$$E_{\sigma 1} = 4.44 f w_1 \Phi_{\sigma 1 m}; E_{\sigma 2} = 4.44 f w_2 \Phi_{\sigma 2 m}$$

$$\left. \begin{aligned} \dot{U}_1 + \dot{E}_1 &= \dot{I}_1 r_1 + j \dot{I}_1 x_1 \\ \dot{U}_2 &= \dot{E}_2 - \dot{I}_2 r_2 - j \dot{I}_2 x_2 \\ \dot{I}_1 &= \dot{I}_0 + (-\dot{I}_2) \end{aligned} \right\}$$

$$E_{\sigma 1} = I_1 x_1; E_{\sigma 2} = I_2 x_2$$

$$\dot{E}_{\sigma 1} = -j \dot{I}_1 x_1; \dot{E}_{\sigma 2} = -j \dot{I}_2 x_2$$

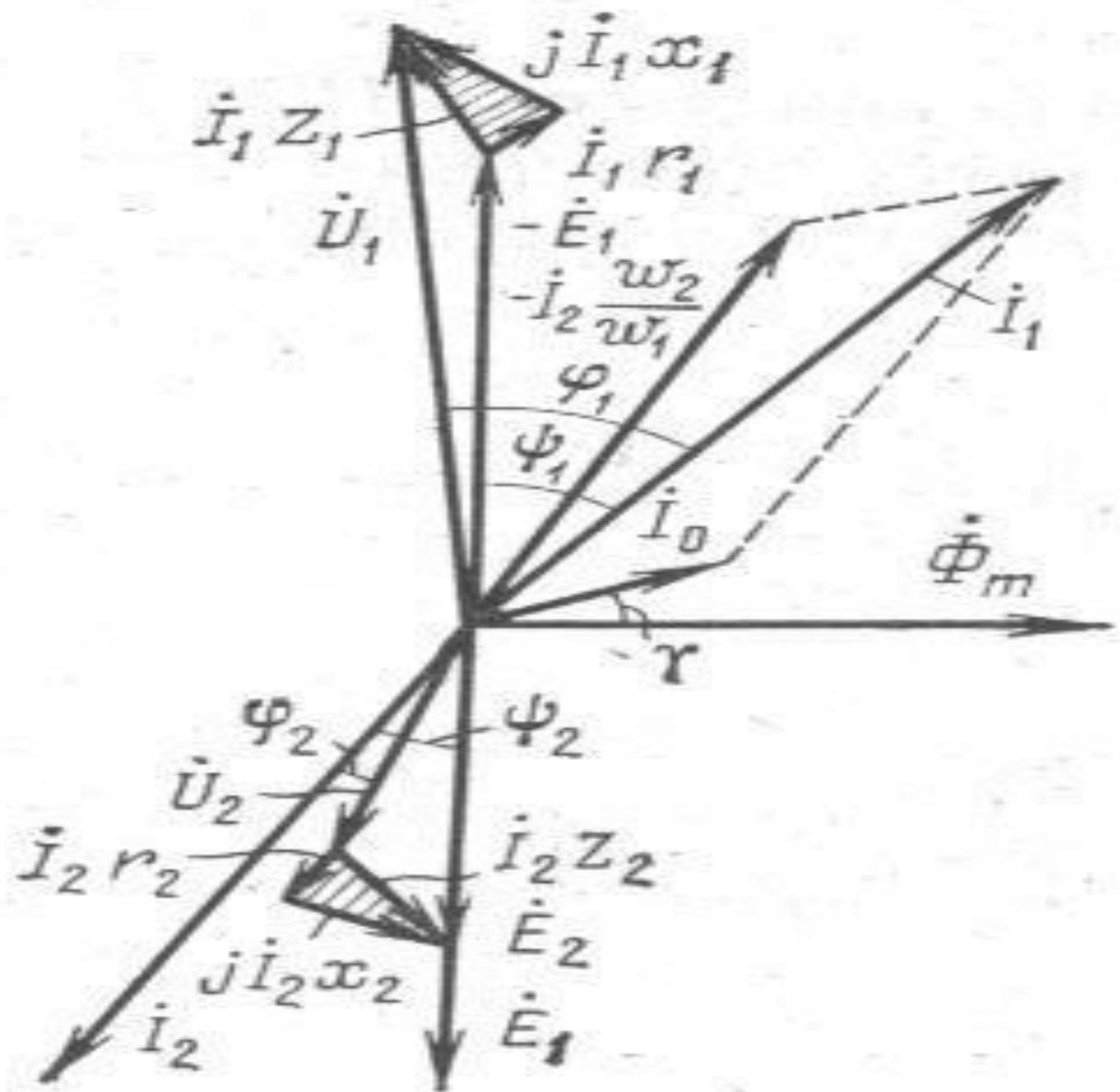
$$\dot{U}_1 + \dot{E}_1 = \dot{I}_1 R_1 + j \dot{I}_1 x_1 = \dot{I}_1 Z_{-1} \quad (1)$$

$$\dot{E}_2 = \dot{I}_2 R_2 + j \dot{I}_2 x_2 + \dot{I}_2 Z_{-H} = \dot{I}_2 Z_2 + \dot{I}_2 Z_H \quad (2)$$

$$\dot{I}_1 + \left(-I_2 \frac{w_2}{w_1} \right) = \dot{I}_0 \quad (3)$$

$$\dot{U}_2 = \dot{I}_2 Z_{-H}$$

$$\dot{U}_2 = \dot{E}_2 - \dot{I}_2 R_2 - j \dot{I}_2 x_2$$

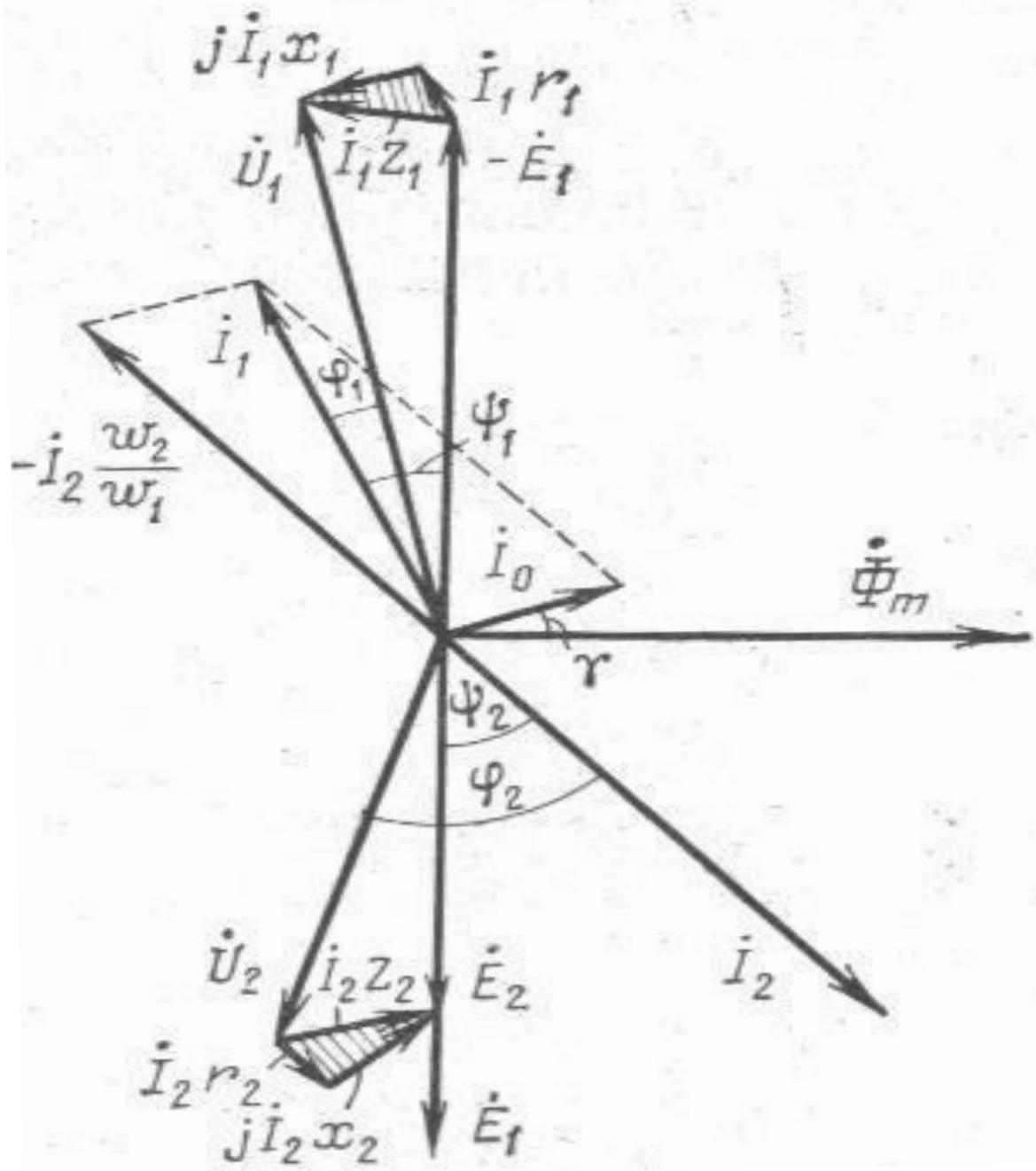


$$\dot{I}_{2p} \omega_2 = \dot{I}_2 \omega_2 \sin \varphi_2, \text{ где } \dot{I}_2 = I_2 \sin \psi_2$$

$$\dot{\Phi}_m = \frac{E_1}{4,44 f \omega_1}$$

$$\gamma = 5 \cdot 10^0$$

$$\psi = \arctg \frac{x_2 + x_H}{r_2 + r_H}$$



Составление схемы замещения

$$\begin{aligned} E_1 &= \\ kE_2 & \\ E_1 &= I_0 Z_m = I_0 (R_m + jx_m) \end{aligned}$$

$$E_1 \approx U_1 \quad I_0 = \frac{E_1}{R_m + x_m} = \frac{E_1}{Z_m}$$

$$I_0 E_1 \cos \varphi_0 = I_0 R_m^2$$

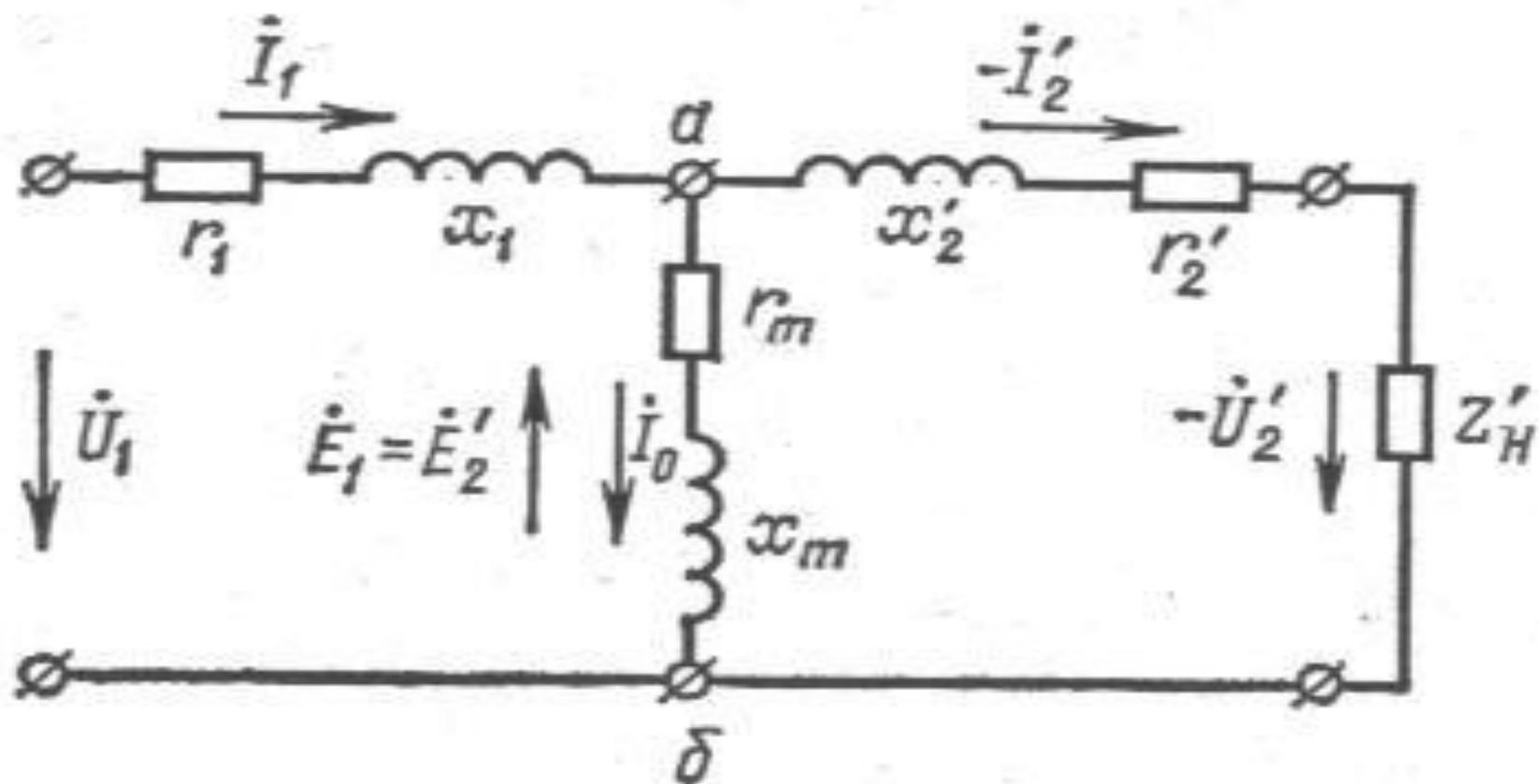
$$\dot{I}_1 = \frac{\dot{U}_1}{Z_1 + [Z_m(k^2 Z_H + k^2 Z_2)] / [Z_m + (k^2 Z_H + k^2 Z_2)]} = \frac{\dot{U}_1}{Z_{\text{экв}}}$$

$$Z_{\text{экв}} = Z_1 + \frac{Z_m(Z'_H + Z'_2)}{Z_m + Z'_H + Z'_2}$$

$$Z_1 = R_1 + jx_1, Z_m = R_m + jx_m, Z'_H = k^2 Z_H$$

$$Z'_2 = k^2 Z_2 = k^2 (R_2 + jx_2)$$

$$R'_2 = R_2 k^2, x'_2 = x_2 k^2$$



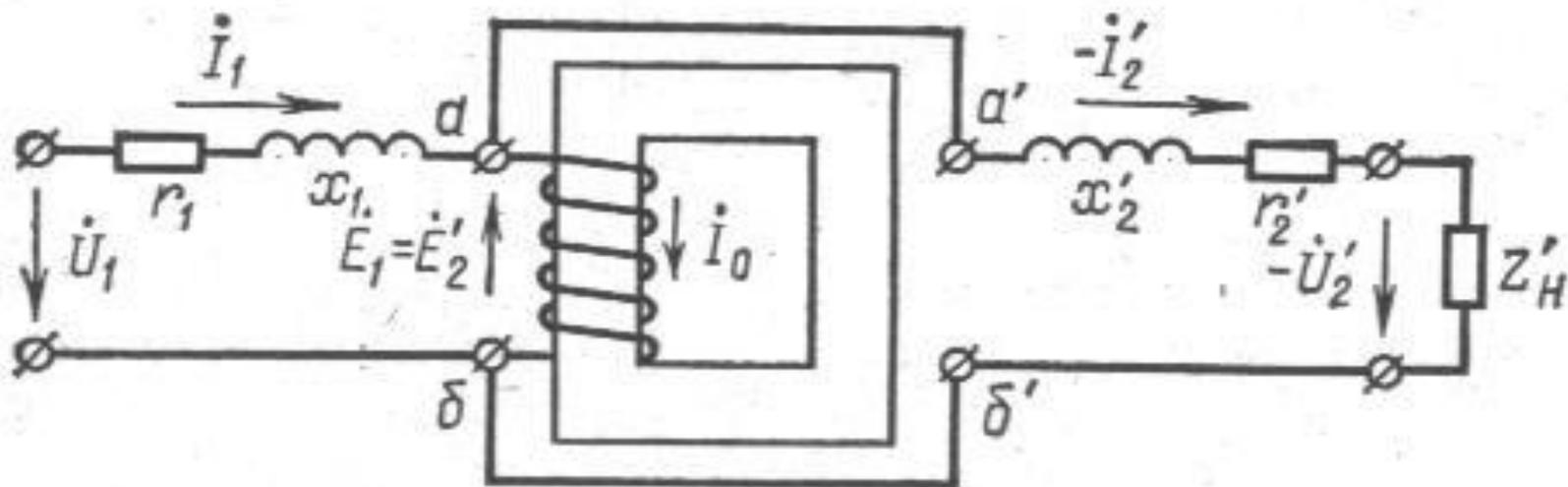
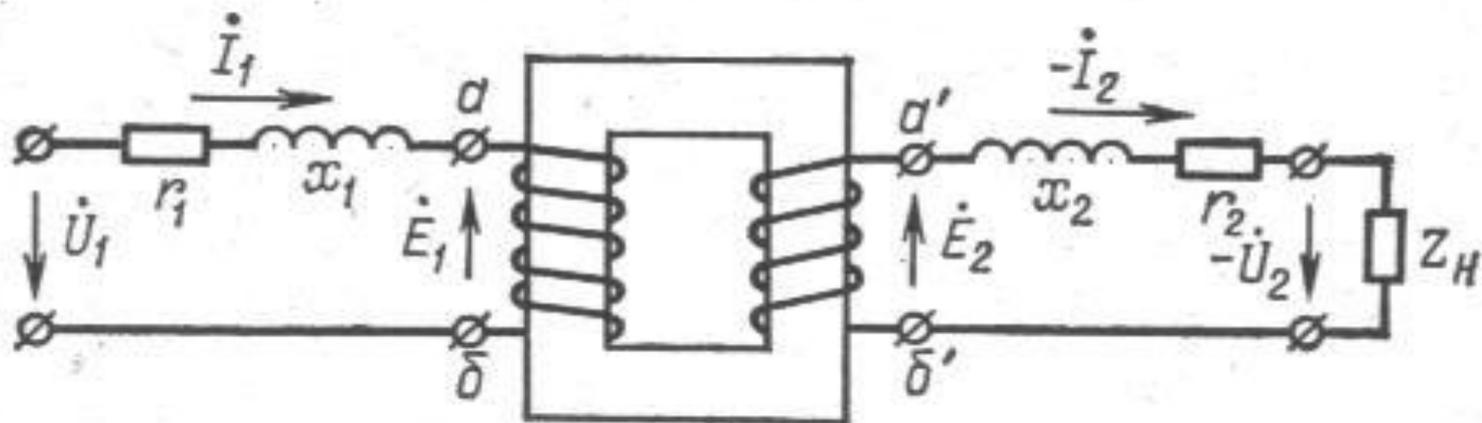
$$E_2' = kE_2 = E_1, I_2' = \frac{I_2}{k}$$

$$I_2' E_2' = \frac{I_2}{k} kE_2 = I_2 E_2$$

$$I_2'^2 R_2' = \left(\frac{I_2}{k}\right)^2 R_2 k^2 = I_2^2 R_2$$

$$\frac{I_2' R_2'}{E_2'} = \frac{\left(\frac{I_2}{k}\right) k^2 R_2}{kE_2} = \frac{I_2 R_2}{E_2}$$

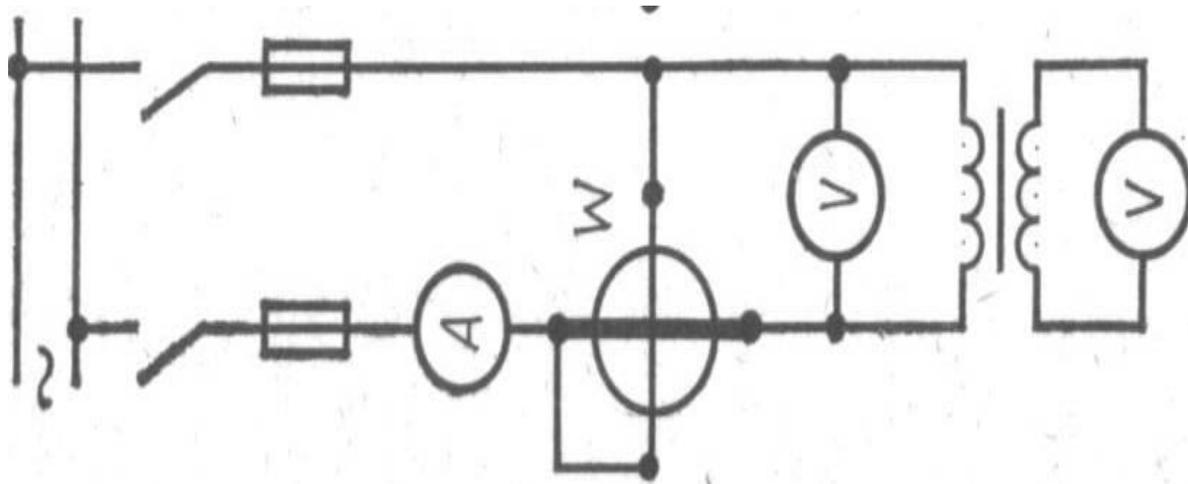
$$\frac{I_2' x_2'}{E_2'} = \frac{\left(\frac{I_2}{k}\right) k^2 x_2}{kE_2} = \frac{I_2 x_2}{E_2}$$



Определение параметров схемы замещения по опытам холостого хода и короткого замыкания

Опыт холостого

хода



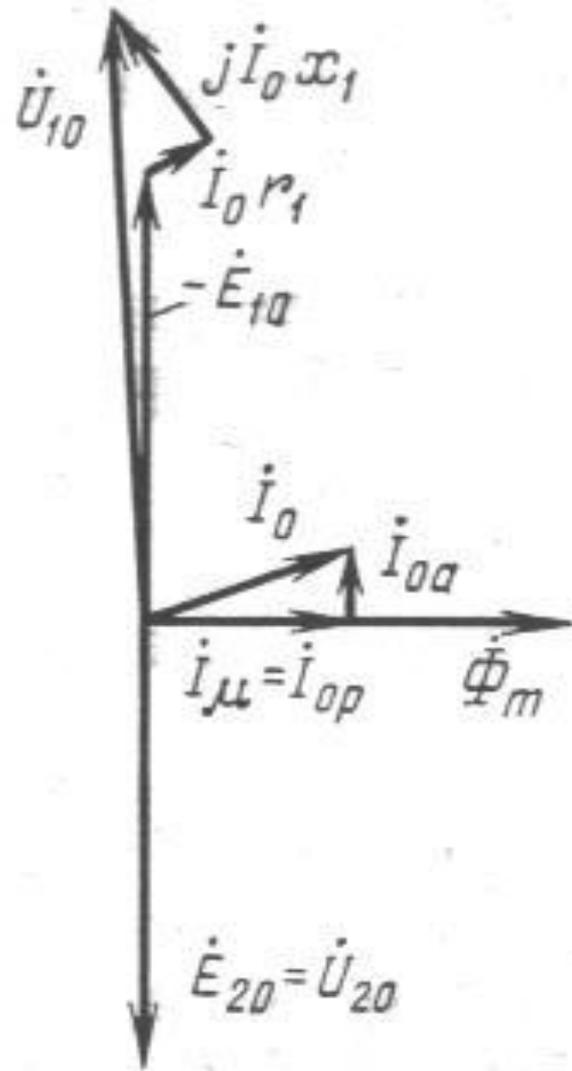
$$\left. \begin{aligned} Z_1 + Z_m &= \frac{U_0}{I_0}; R_1 + R_m = \frac{P_0}{I_0^2} \\ x_1 + x_m &= \sqrt{(Z_1 + Z_m)^2 - (R_1 + R_m)^2} \end{aligned} \right\}$$

$$P_0 = I_0^2 (R_1 + R_m) \approx I_0^2 R_m \Rightarrow R_m = \frac{P_0}{I_0^2}$$

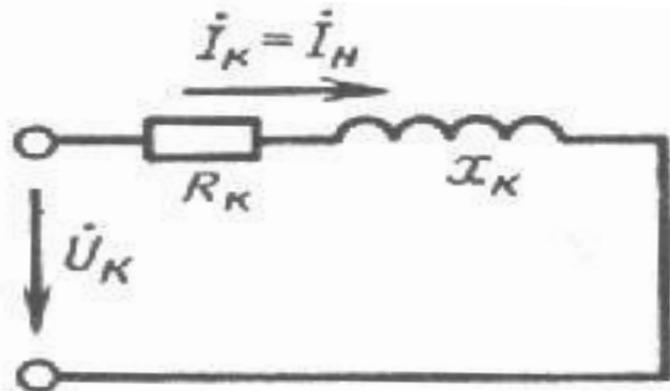
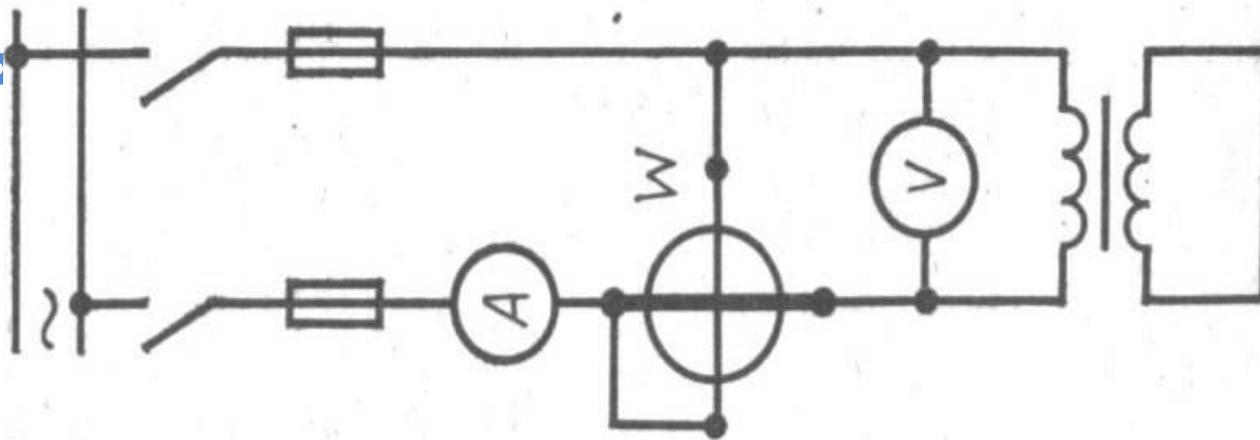
$$Z_m = \frac{U_0}{I_0} \quad x_m = \sqrt{Z_m^2 - R_m^2}$$

$$k = \frac{U_0}{U_{20}}$$

$$\dot{U}_0 = -\dot{E}_{10} + I_0 \dot{R}_1 + j I_0 \dot{x}_1$$



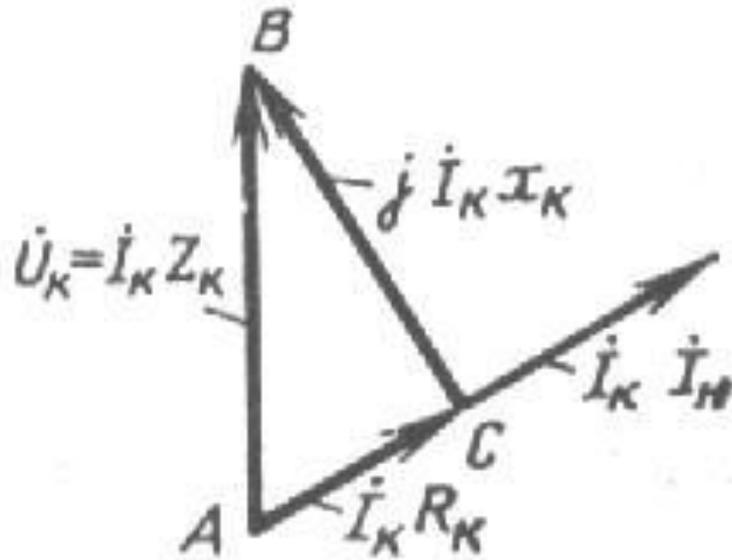
Опыт короткого замыкания



$$Z_k = Z_1 + Z_2' = \frac{U_k}{I_{HOM}};$$

$$R_k = R_1 + R_2' = \frac{P_k}{I_{HOM}^2};$$

$$x_k = x_1 + x_2' = \sqrt{Z_k^2 - R_k^2};$$



$$U_k = \left(\frac{I_{HOM} Z_k}{U_{HOM}} \right) \cdot 100\%$$

$$U_{ka} \% = \left(\frac{I_{HOM} R_k}{U_{HOM}} \right) \cdot 100\%$$

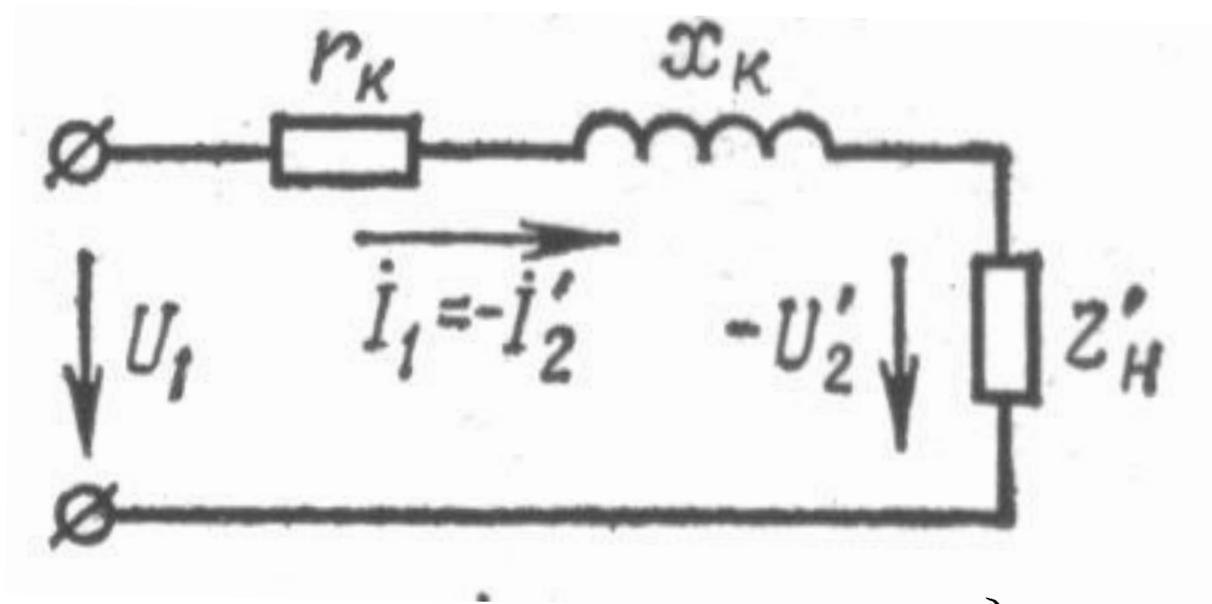
$$U_{kp} \% = \left(\frac{I_{HOM} x_k}{U_{HOM}} \right) \cdot 100\%$$

$$U_{ka} = U_k \cos \varphi_k$$

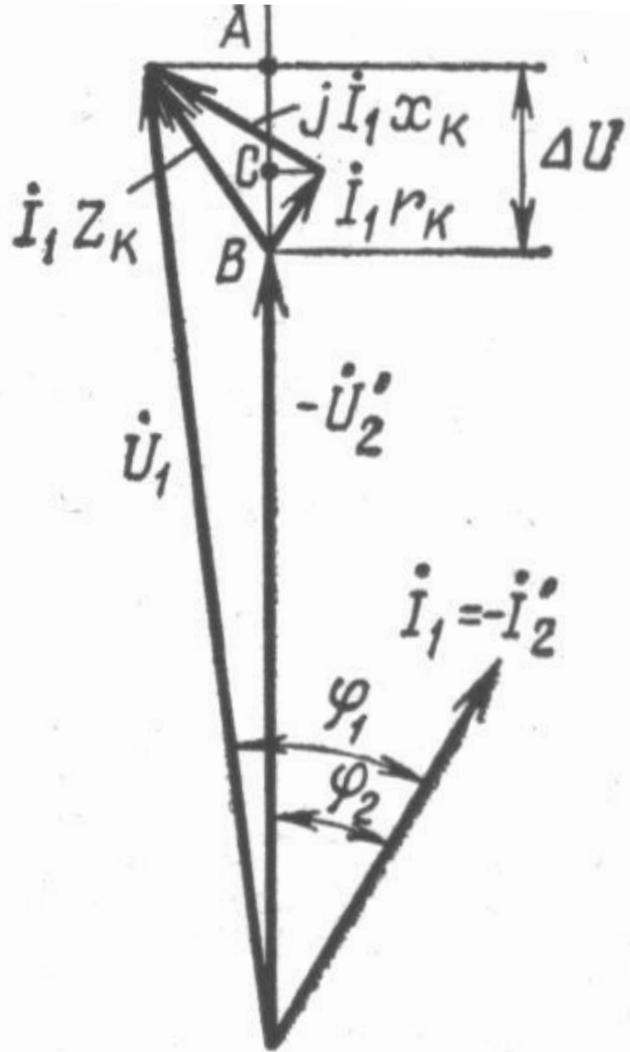
$$U_{kp} = U_k \sin \varphi_k$$

$$U_k = \sqrt{U_{ka}^2 + U_{kp}^2}$$

Упрощенная схема замещения трансформатора



$$\left. \begin{aligned} Z_k &= Z_1 + Z_2' = \frac{U_k}{I_{HOM}}; \\ R_k &= R_1 + R_2' = \frac{P_k}{I_{HOM}^2}; \\ x_k &= x_1 + x_2' = \sqrt{Z_k^2 - R_k^2}; \end{aligned} \right\}$$



$$\dot{I}_1 Z_k = \dot{I}_1 R_k + j \dot{I}_1 x_k$$

$$I_1 Z_k = \frac{\beta U_k \% U_{HOM}}{100}$$

$$I_1 R_k = \frac{\beta U_{ka} \% U_{HOM}}{100}$$

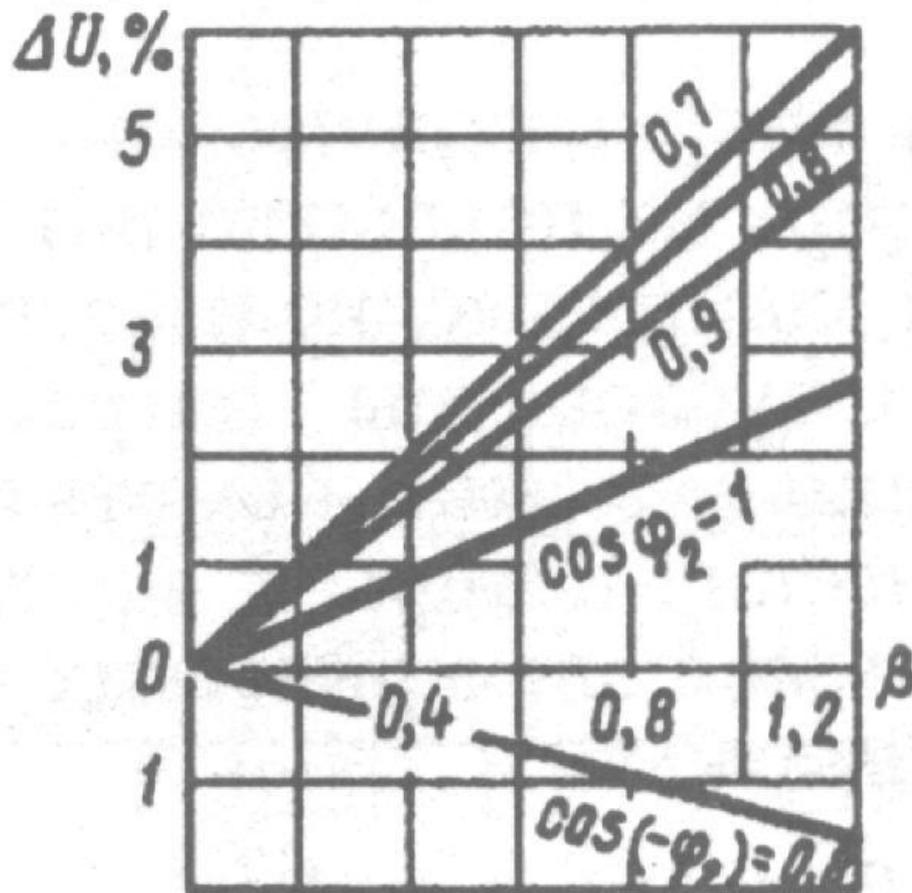
$$I_1 x_k = \frac{\beta U_{kp} \% U_{HOM}}{100}$$

$$\beta = \frac{I_2}{I_1} \approx \frac{I_1}{I_{1HOM}}$$

$$\Delta U \% = \frac{U_{20} - U_2}{U_{20}} 100 \% = \frac{U_{1H} - U_2'}{U_{1H}} 100 \%$$

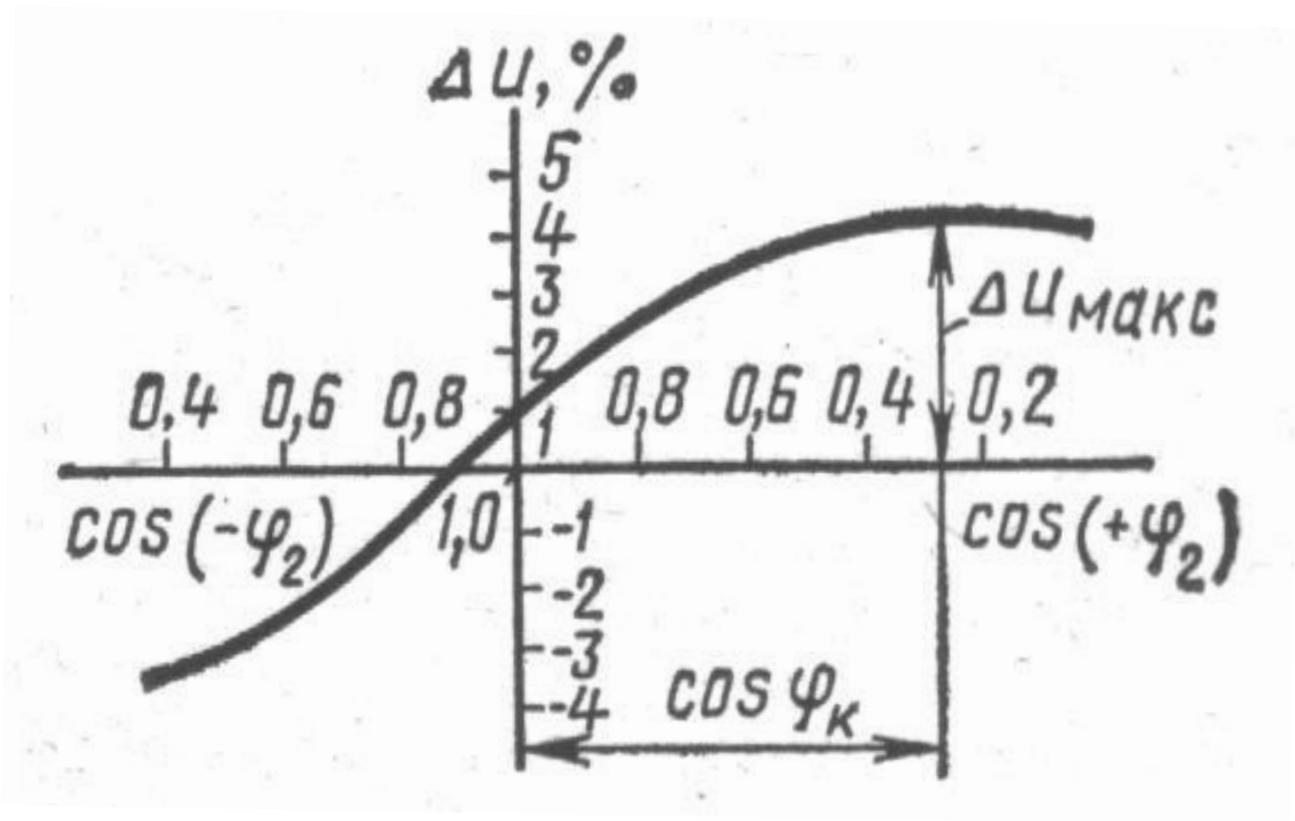
Внешние характеристики

$U_2 = f(I_2)$ или $U_2 = f(\beta)$ при $U_1 = U_{НОМ} = const$ и $f = f_{НОМ} = const$ и $\cos\varphi_2 = const$



$\Delta U = f(\beta)$ при $\cos\varphi_2 = const$

$$\Delta U = f(\cos \varphi_2) n p u \beta = \text{const}$$

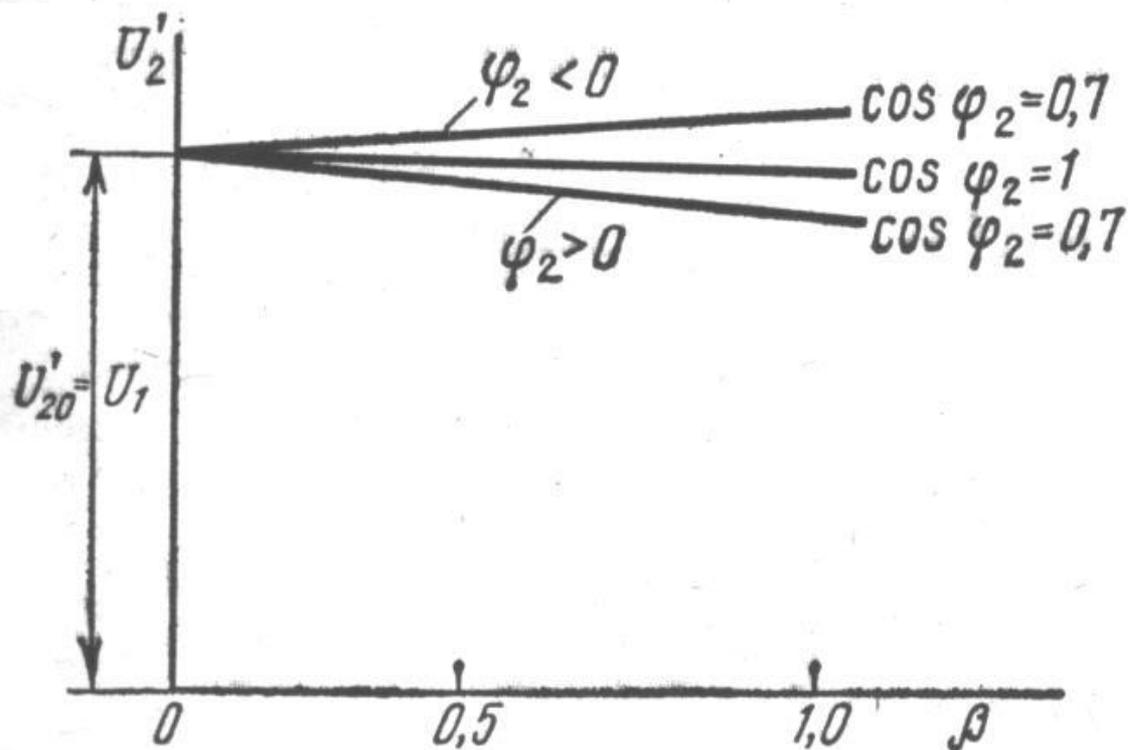


$$U_2 = f(\beta)$$

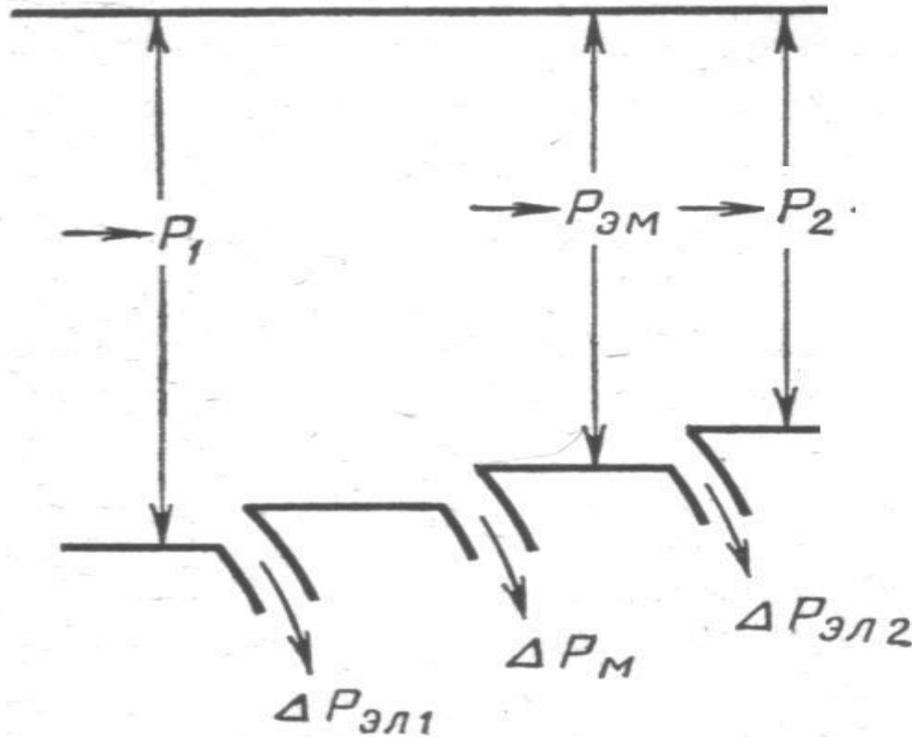
$$U_{ka} = U_k \cos \varphi_k;$$

$$U_{kp} = U_k \sin \varphi_k$$

$$\Delta U = \beta U_k (\cos \varphi_k \cos \varphi_2 + \sin \varphi_k \sin \varphi_2) = \beta U_k \cos(\varphi_k - \varphi_2)$$



Энергетическая



$$\Delta P_2 = P_1 - \Delta P_{эл1} - \Delta P_{эл2} -$$

$$P_{эм} = P_1 - \Delta P_{эл1} -$$

$$\Delta P_{м}$$

$$\eta = \frac{P_2}{P_1} = \frac{U_2 I_2 \cos \varphi_2}{U_1 I_1 \cos \varphi_1}$$

$$\eta = \frac{P_1 - \Delta P}{P_1} = 1 - \frac{\Delta P}{P_2 + \Delta P}$$

$$\eta = \frac{P_2}{P_2 + \Delta P_{\text{ЭЛ1}} + \Delta P_{\text{ЭЛ2}} + \Delta P_M} = 1 - \frac{\Delta P_{\text{ЭЛ1}} + \Delta P_{\text{ЭЛ2}} + \Delta P_M}{P_2 + \Delta P_{\text{ЭЛ1}} + \Delta P_{\text{ЭЛ2}} + \Delta P_M}$$

$$I_2' = I_1 \Rightarrow \Delta P_{\text{ЭЛ}} = \Delta P_{\text{ЭЛ1}} + \Delta P_{\text{ЭЛ2}} = I_1^2 R_1 + I_2'^2 R_2 \approx I_2'^2 (R_1 + R_2') \approx I_2'^2 R_k$$

$$\Delta P_{\text{ЭЛ}} \approx \beta^2 I_{2\text{НОМ}}'^2 R_k \approx \beta^2 \Delta P_{\text{ЭЛ.НОМ}}$$

$$\Delta P_{\text{ЭЛ.НОМ}} \approx I_{2\text{НОМ}}'^2 R_k \approx I_{1\text{НОМ}}'^2 R_k$$

$$\Delta P_{\text{ЭЛ}} = \beta^2 P_K$$

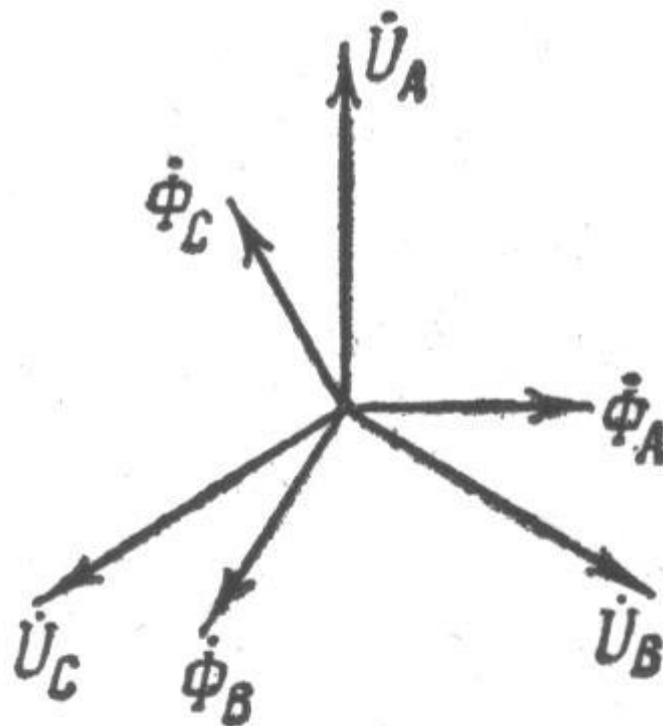
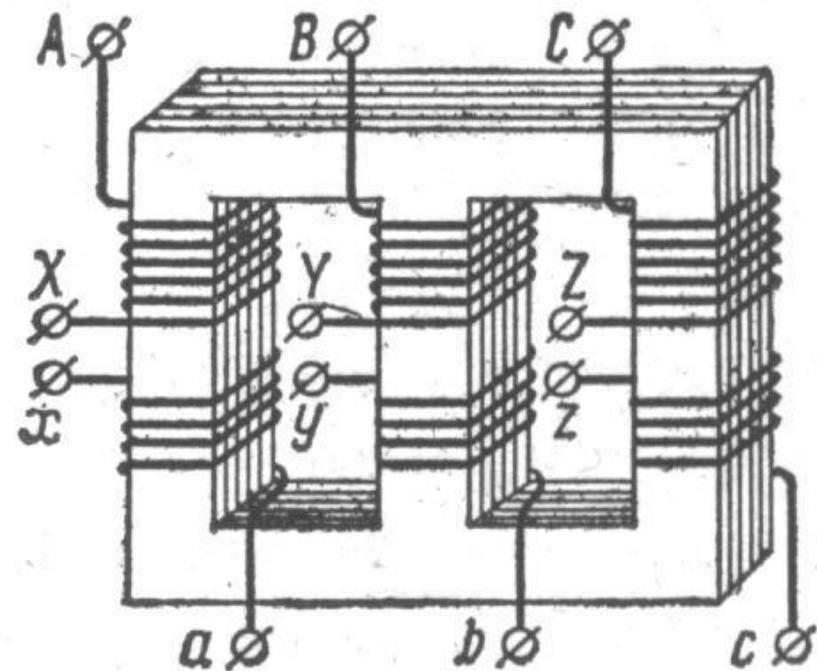
$$\Delta P = P_0 + \beta^2 P_K$$

$$P_2 = I_2 U_2 \text{Cos} \varphi_2 \approx \beta S_{\text{НОМ}} \text{Cos} \varphi_2$$

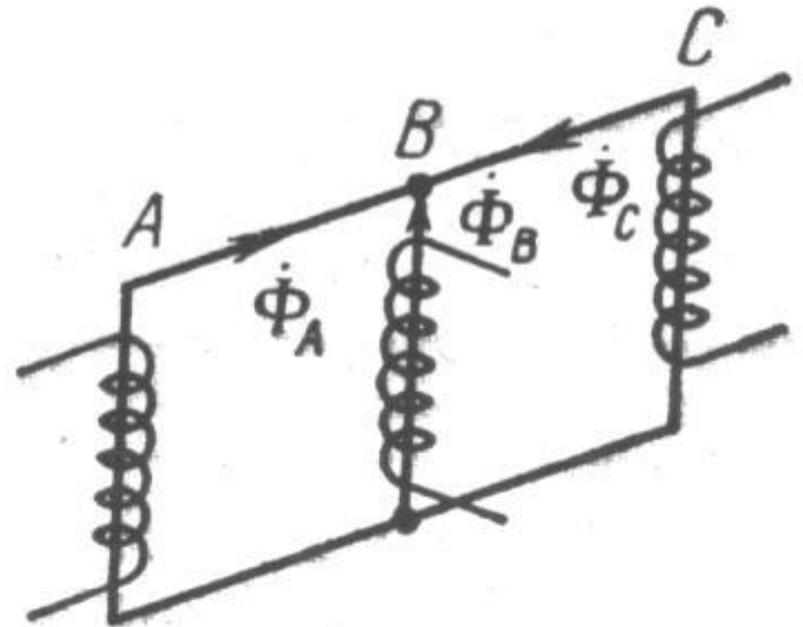
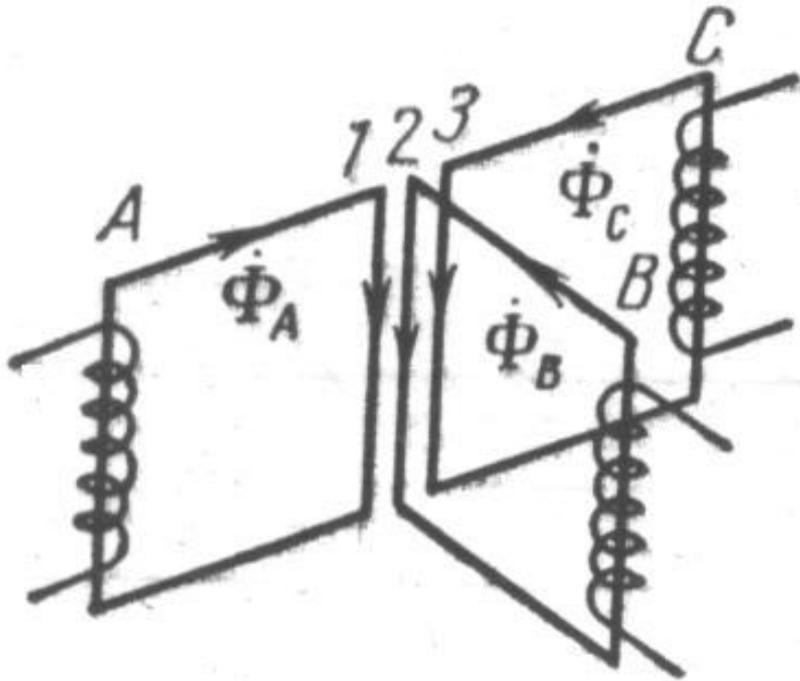
$$\eta = 1 - \frac{\beta^2 P_K + P_0}{\beta S_{\text{НОМ}} \text{Cos} \varphi_2 + \beta^2 P_K + P_0}$$

$$P_{0\text{НОМ}} = \beta'^2 P_{K\text{НОМ}} \quad \beta' = \sqrt{\frac{P_{0\text{НОМ}}}{P_{K\text{НОМ}}}} \quad \eta = \frac{W_2}{W_1}$$

Трехфазные трансформаторы



Трехстержневой 3-фазный трансформатор



$$\dot{\Phi}_{PE3} = \dot{\Phi}_A + \dot{\Phi}_B + \dot{\Phi}_C$$

Схемы соединений

**A, B, C; X, Y,
Z**

$$K_{\Phi} = \frac{W_{BH}}{W_{HH}} = \frac{U_{0\Phi BH}}{U_{0\Phi HH}}$$

$$K_L = \frac{U_{0L BH}}{U_{0L HH}}$$

**a, b, c, x, y,
z**

Y/Y, Δ /Δ

**Y/
Δ**

Δ/Y

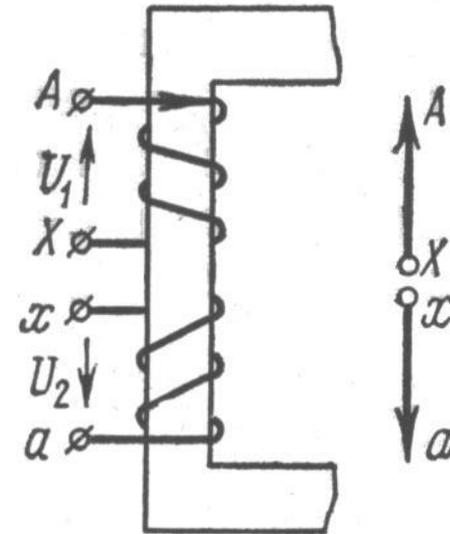
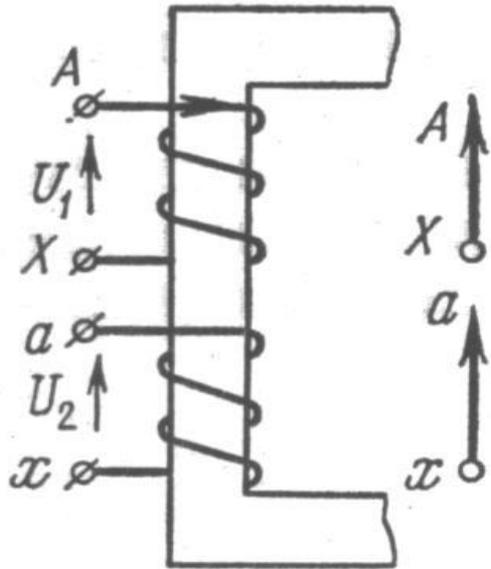
O

$K_L = K_{\Phi}$

$$K_L = \sqrt{3} K_{\Phi}$$

$$K_L = \frac{K_{\Phi}}{\sqrt{3}}$$

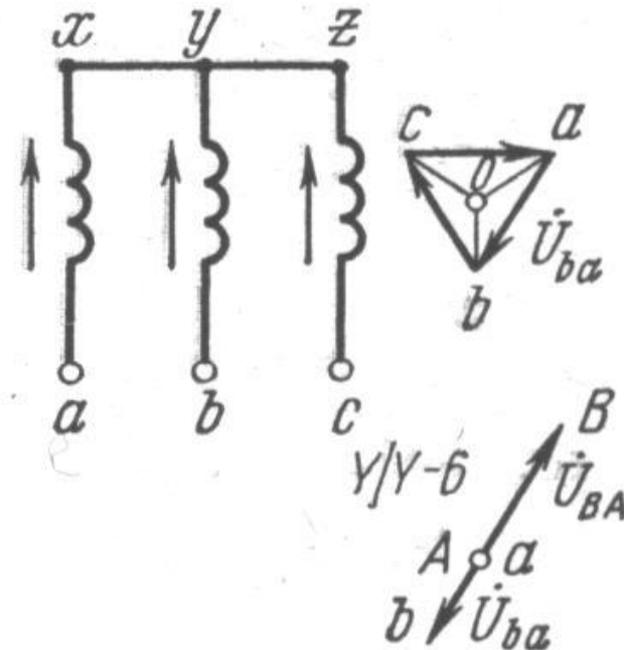
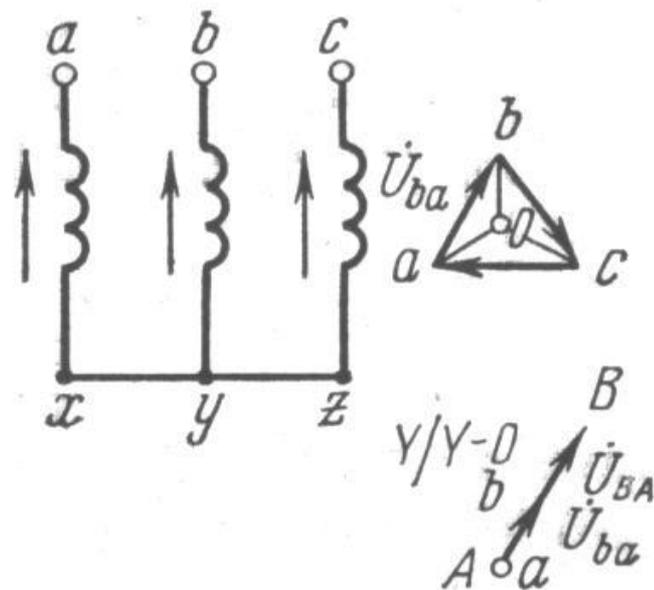
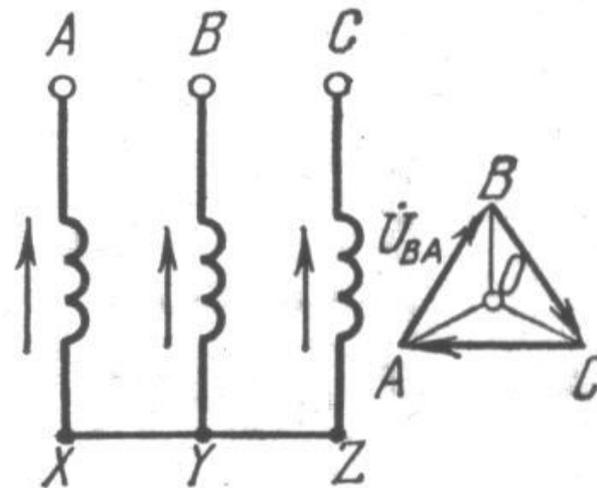
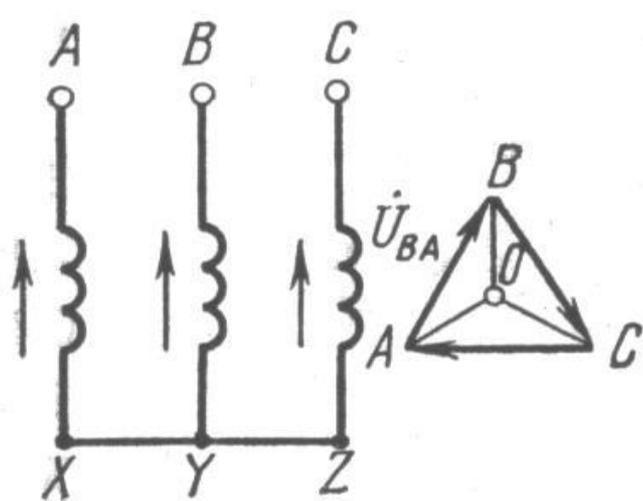
Группы соединений обмоток трансформаторов

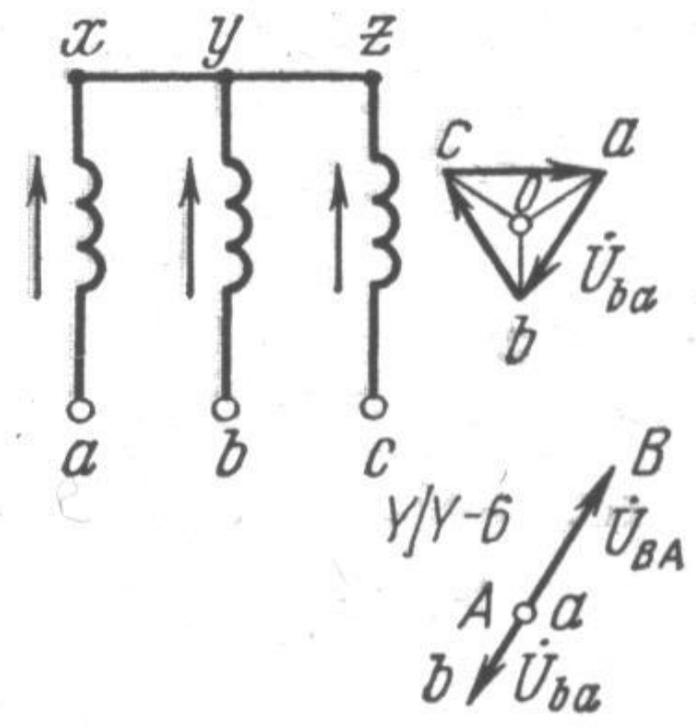
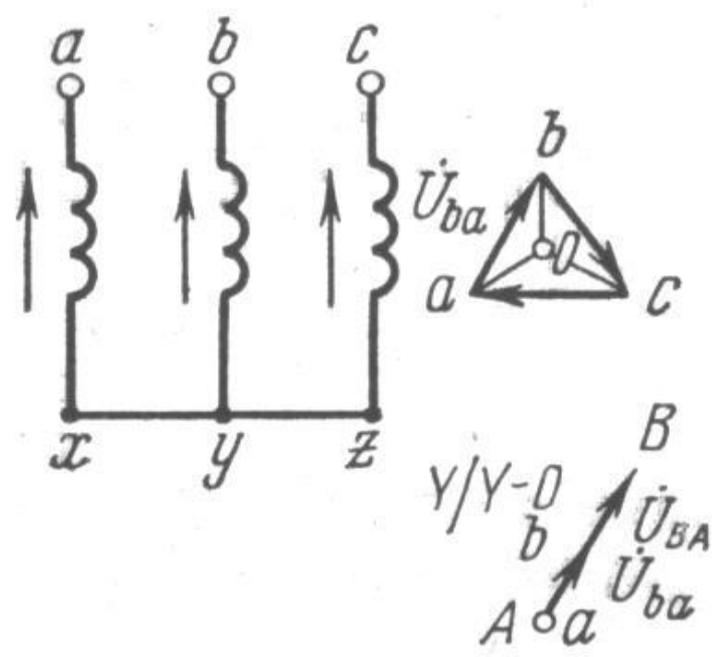
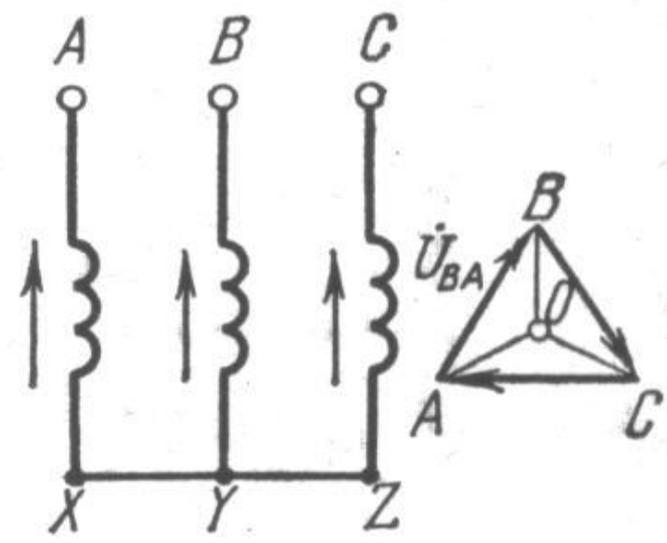
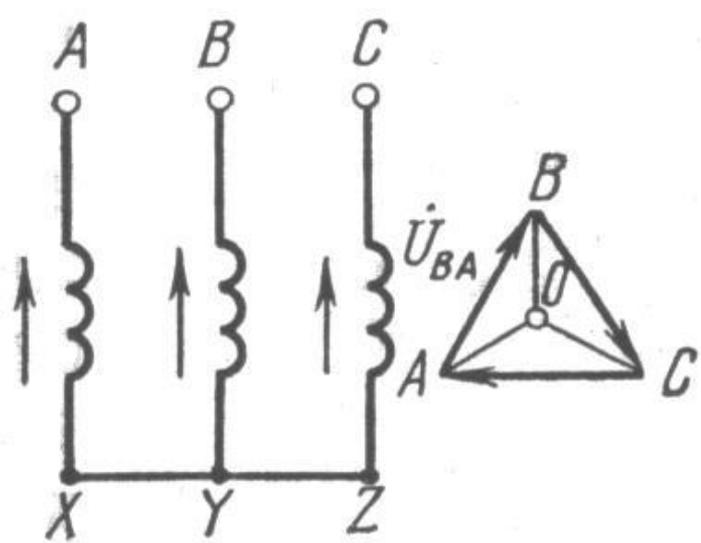


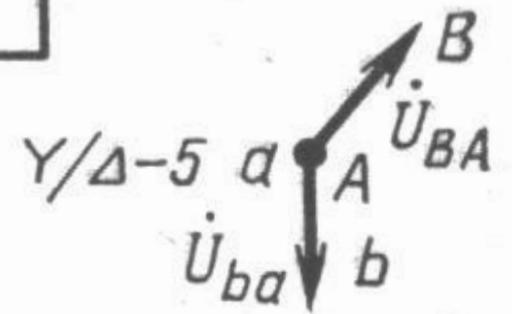
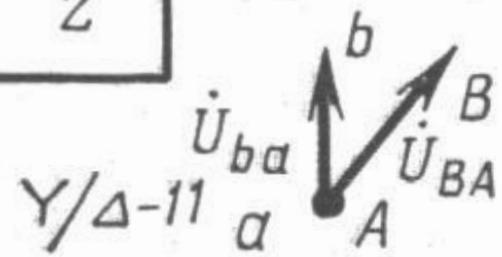
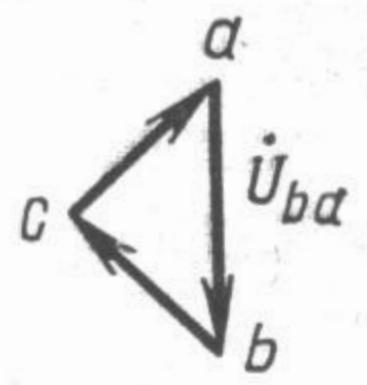
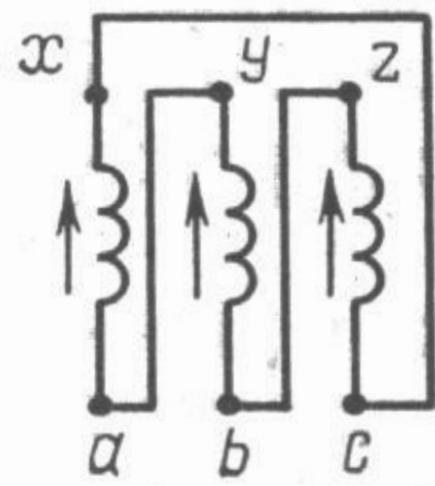
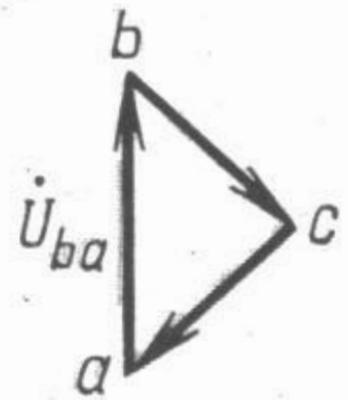
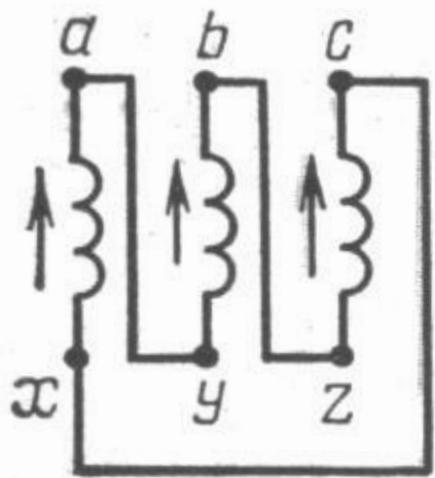
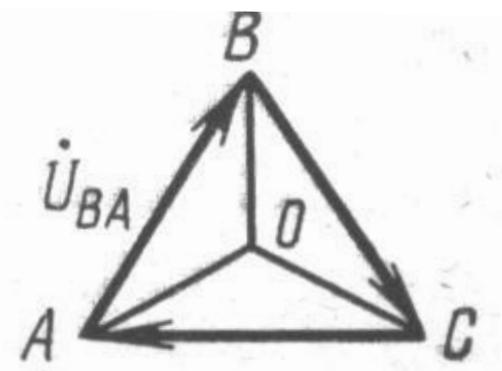
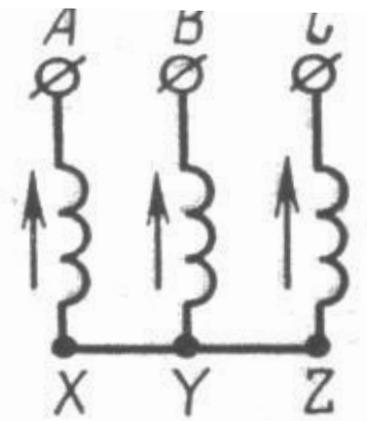
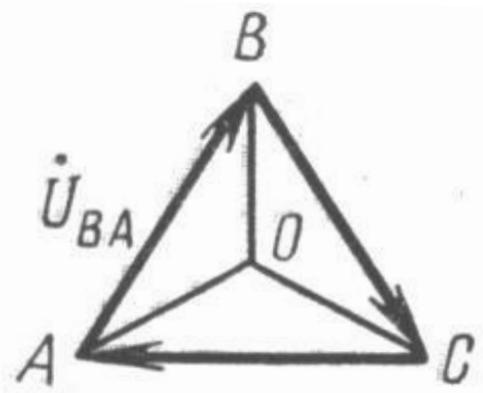
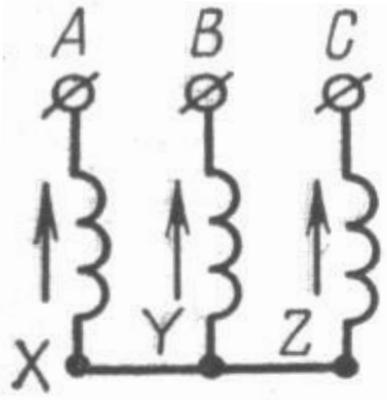
Номер группы определяют величиной угла, на который вектор линейного напряжения обмотки НН отстает от вектора линейного напряжения обмотки ВН.

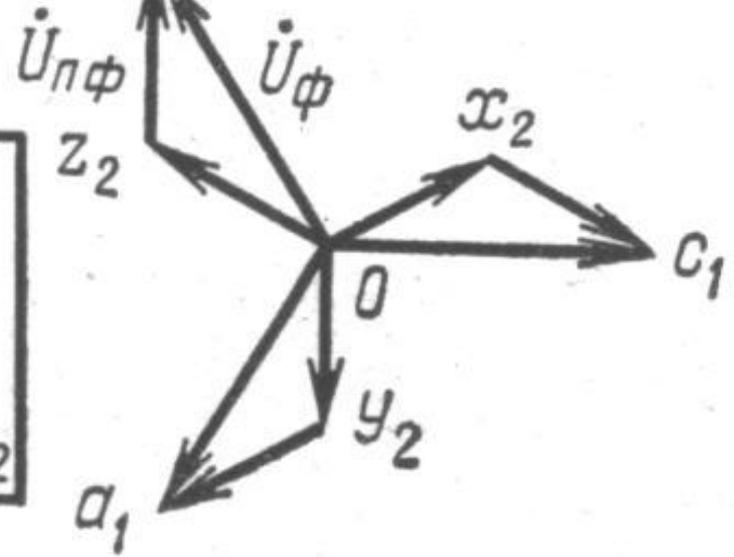
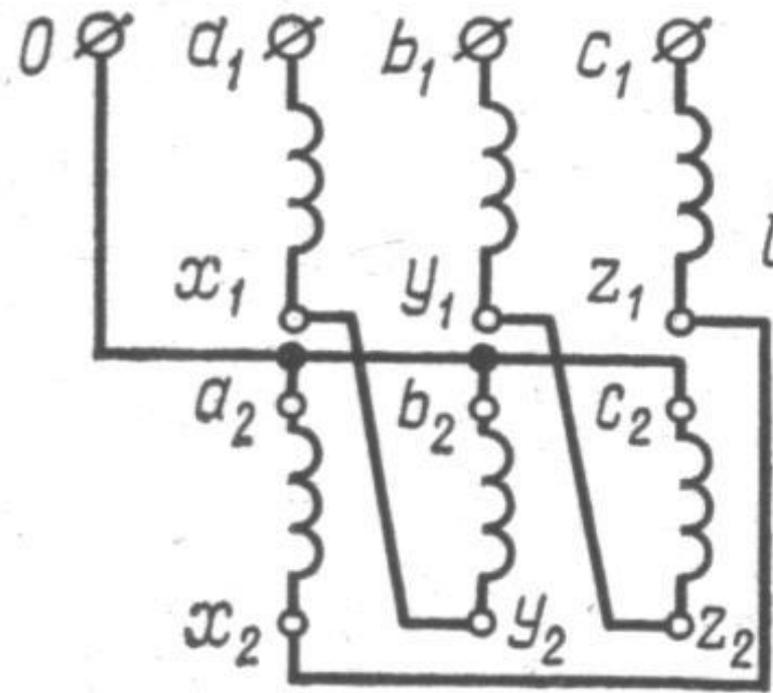
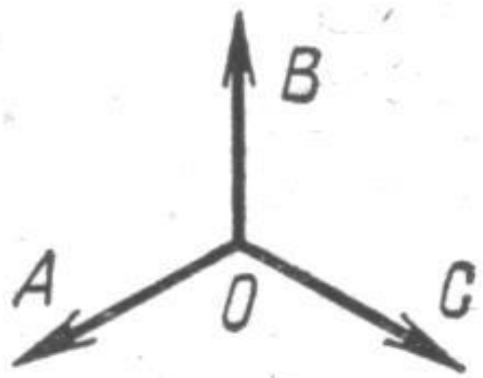
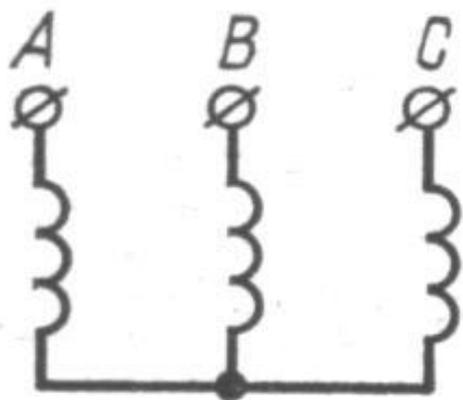
Для определения номера группы этот угол следует разделить на 30° .

Трехфазные трансформаторы

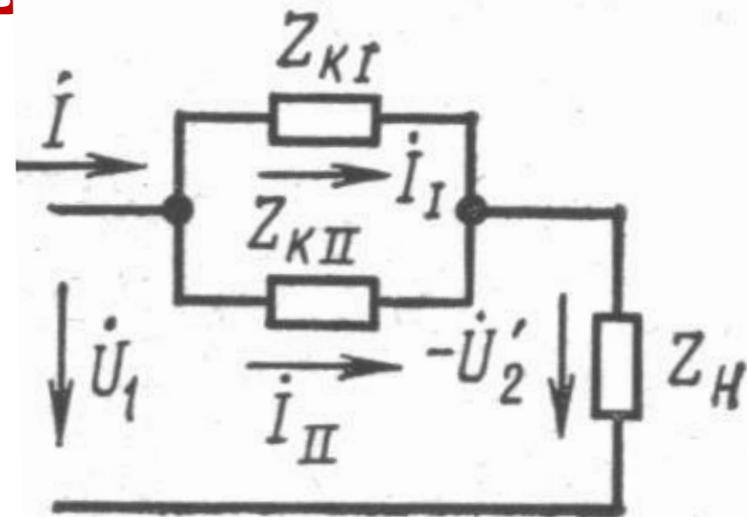
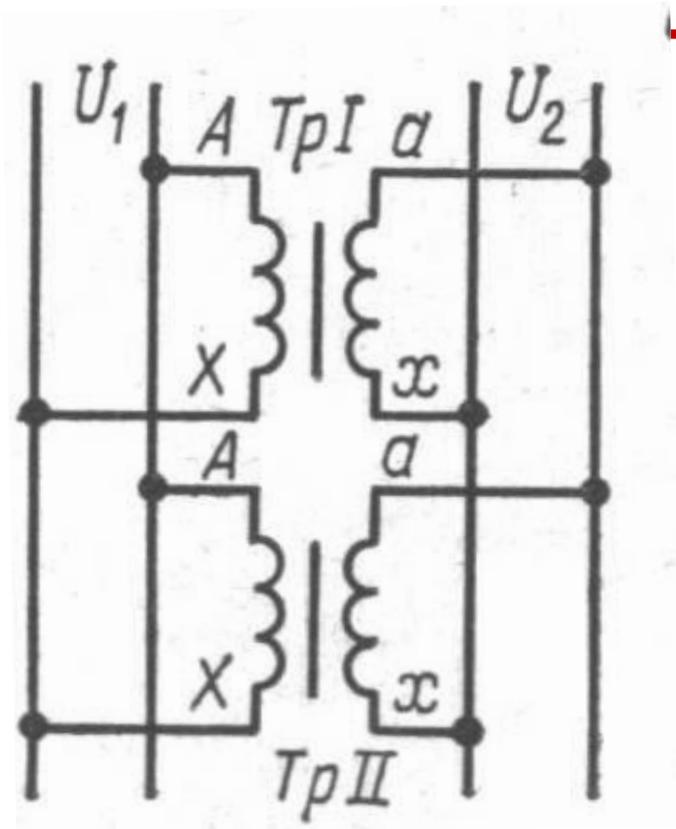








Параллельная работа торов

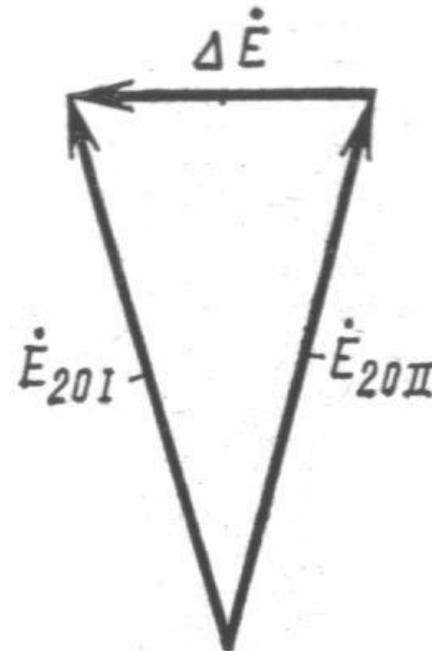


$$\dot{I}_{УР} = \frac{\dot{E}_{20I} - \dot{E}_{20II}}{Z_{-KI} + Z_{-KII}}$$

1. Равенство вторичных ЭДС

2. Совпадение по фазе ЭДС

$$\dot{E}_{20I} \quad \dot{E}_{20II}$$



3. Распределение нагрузок в соответствии с номинальной мощностью

$$\dot{I}_I Z_{-KI} = \dot{I}_{II} Z_{-KII} = \dot{I}_{III} Z_{-KIII} = \dots = \dot{I}_n Z_{-Kn}$$

$$\frac{I_I}{I_{II}} = \frac{Z_{KII}}{Z_{KI}} \quad I_I : I_{II} = \frac{1}{Z_{KI}} : \frac{1}{Z_{KII}}$$

$$I_I : I_{II} = \frac{I_{HOMI}}{I_{HOMI} Z_{KI}} : \frac{I_{HOMII}}{I_{HOMII} Z_{KII}} \quad U_2 \cos \varphi_2 \quad \frac{U_{HOM}^2}{100}$$

$$P_1 : P_2 = \frac{S_{HOMI}}{U_{KI}} : \frac{S_{HOMII}}{U_{KII}}$$

$$\frac{P_1}{S_{HOMI}} : \frac{P_2}{S_{HOMII}} = \frac{1}{U_{KI}} : \frac{1}{U_{KII}}$$

Автотрансформа

тор

$$E = 4.44 f \Phi_m$$

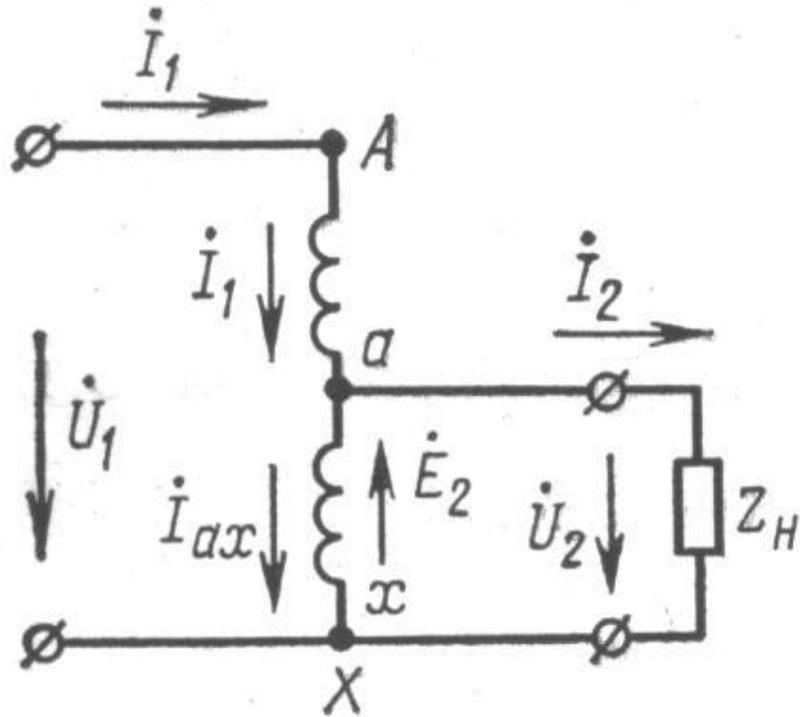
$$U_2 = 4.44 f w_{ax} \Phi_m = U_1 \frac{w_{ax}}{w_{AX}} = \frac{U_1}{K}$$

$$S_H = U_{1H} I_{1H} = U_{2H} I_{2H}$$

$$\frac{U_1}{U_{20}} \approx \frac{E_1}{E_2} = \frac{w_1}{w_2} = k$$

$$I_1 w_1 + I_2 w_2 = 0$$

$$I_{ax} w_2 = I_1 \left(1 - \frac{w_1}{w_2}\right) w_2 = -I_1 (w_1 - w_2)$$



$$I_{ax} = I_2 + I_1$$

$$I_{ax} = I_1 \left(1 - \frac{w_1}{w_2}\right)$$

$$S_{пр} = E_1 I_1 = E_2 I_2$$

$$S_{расч} = E_2 I_a$$

$$S_{пр} = E_2 I_2 = E_2 (I_1 + I_{ax}) = E_2 I_{ax} + E_2 I_1 = S_{ЭМ} + S_{ЭЛ}$$

$$S_{ЭМ} = E_2 I_{ax} = S_{расч}$$

$$S_{ЭЛ} = E_2 I_1$$

$$I_1 = I_2' = \frac{I_2}{K} \quad I_{ax} = I_2 \left(1 - \frac{1}{K}\right)$$

$$S_{расч} = E_2 I_{ax} = E_2 I_2 \left(1 - \frac{1}{K}\right)$$

$$K_{выг} = \frac{S_{расч}}{S_{ПРОХОДНАЯ}} = \left(1 - \frac{1}{K}\right)$$

$$K_{\text{ВЫГ}} = \frac{S_{\text{РАСЧ}}}{S_{\text{ПРОХОДНАЯ}}} = \left(1 - \frac{1}{K}\right)$$

$$\frac{\text{отношение эл.потерь АТР}}{2 - x \text{ обм. тр} - m} \approx \frac{\Delta P_{\text{ЭЛ АТР}}}{\Delta P_{\text{ЭЛ ТР}}} \approx 1 - \frac{1}{K}$$

$$R_{K.ATP} = R_{K.TP} \left(1 - \frac{1}{K}\right);$$

$$X_{K.ATP} = X_{K.TP} \left(1 - \frac{1}{K}\right)$$

Многообмоточные трансформаторы

$$K_{12} = w_{BH} / w_{CH}$$

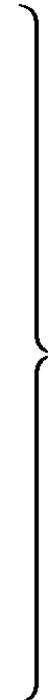
$$K_{13} = w_{BH} / w_{HH}$$

$$\dot{U}_1 = -\dot{E}_1 + \dot{I}_1 R_1 + j \dot{I}_1 x_1$$

$$\dot{U}_2 = \dot{E}_2 - \dot{I}_2 R_2 - j \dot{I}_2 x_2$$

$$\dot{U}_3 = \dot{E}_3 - \dot{I}_3 R_3 - j \dot{I}_3 x_3$$

$$\dot{I}_1 = \dot{I}_0 + \left(-\dot{I}_2 \frac{w_2}{w_1} \right) + \left(-\dot{I}_3 \frac{w_3}{w_1} \right)$$



Регулирование напряжения в трансформаторах