

Economics of pricing and decision making

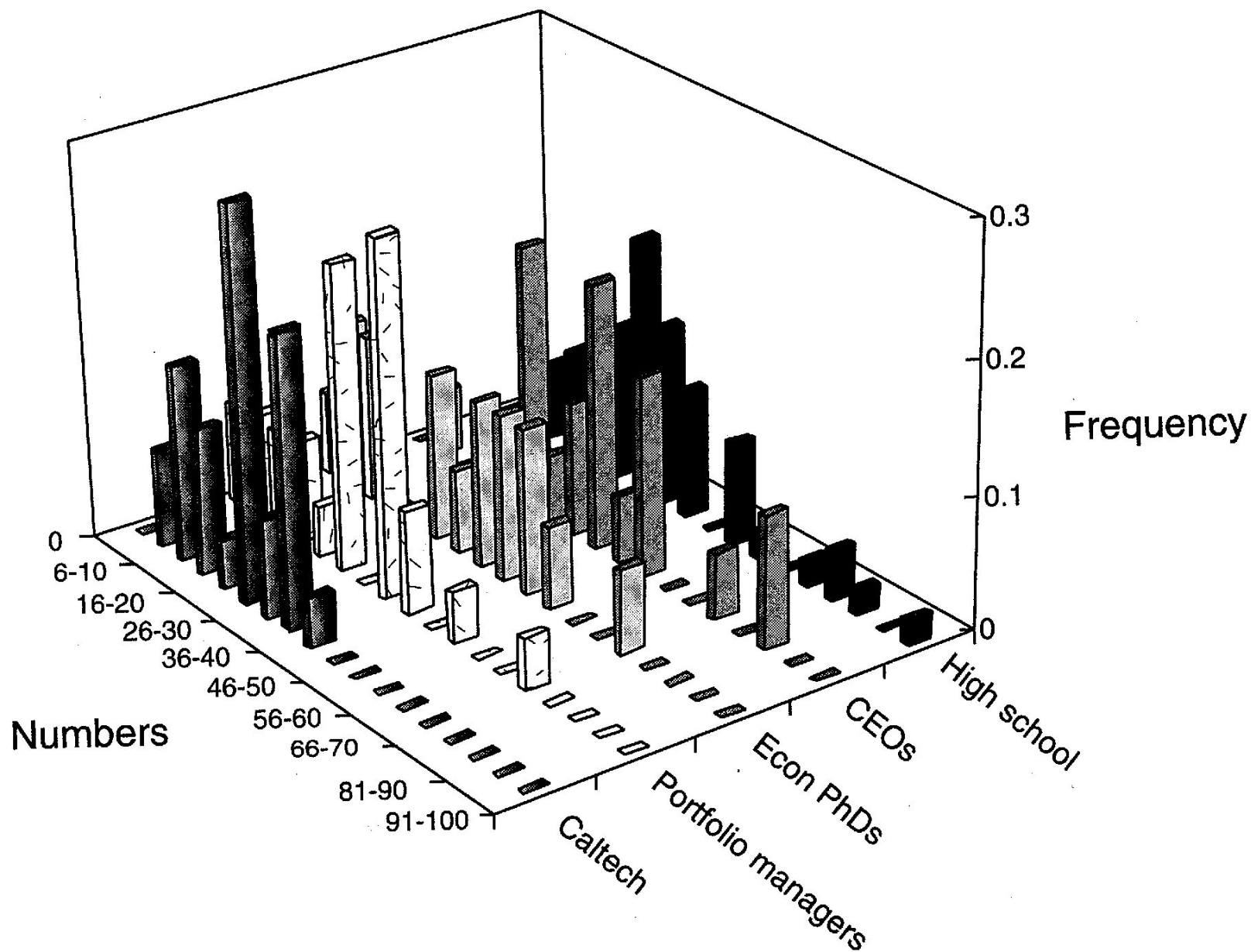
Seminar 1

The guessing game

- Each of you have to declare a number between 0 and 100.

The winner is the person whose number is the closest to $2/3$ of the average of all guesses.

What is your guess?



The guessing game

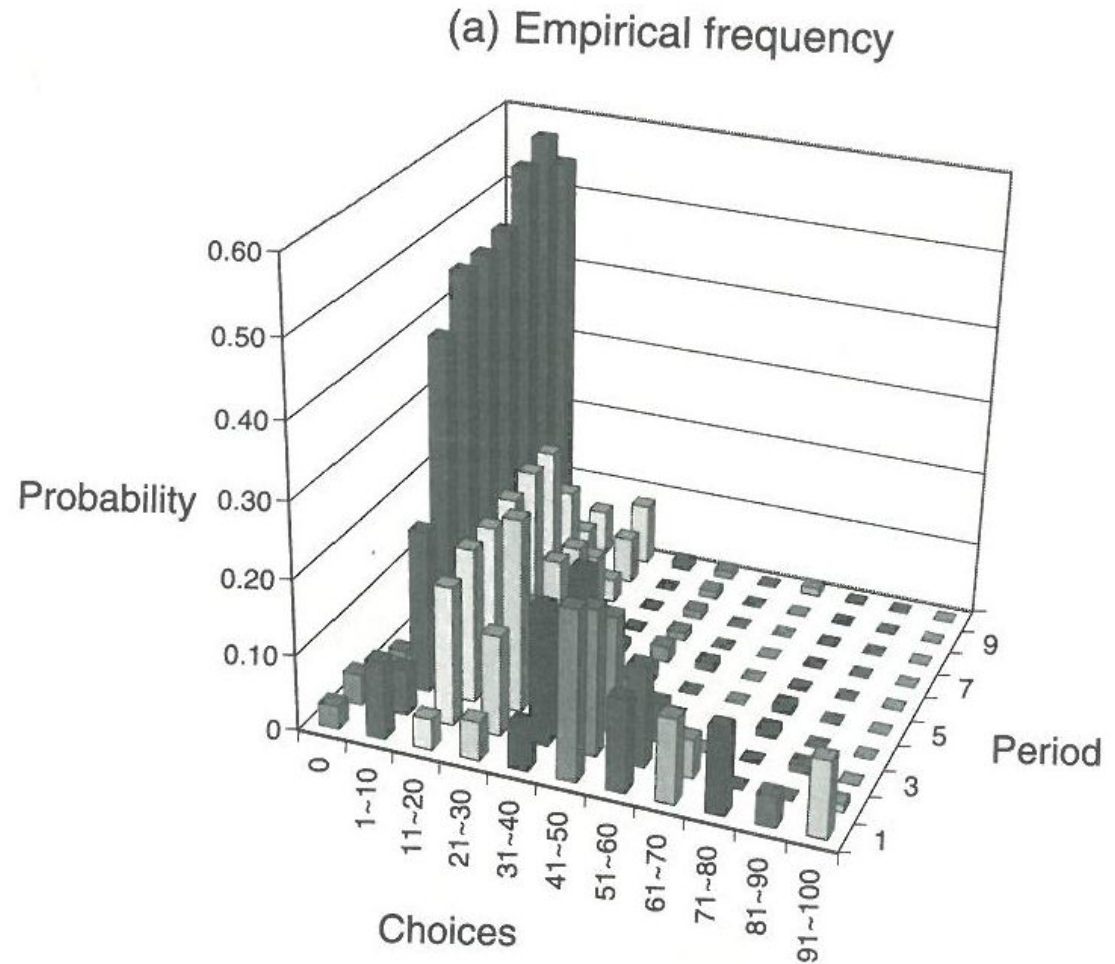
Discussion

- Bounded rationality
 - People do not naturally use deep levels of strategic thinking. They just think 2-3 steps ahead.
- Players may be fully rational, however if a player believes that all other players will say a number $N > 0$, that player will declare $N * 2/3 > 0$.
 - If all players believe that the average guess will be high, this becomes a self-fulfilling prophecy.

The guessing game

Importance of repetition

- When the game is repeated, the average guess eventually goes down to 0.



Q1

		V	W	X	Y	Z
A	9,5	8,7	5,6	3,6	9,2	
B	2,5	7,6	3,5	8,5	0,8	
C	7,3	1,4	5,2	4,1	9,7	
D	5,0	1,6	8,9	0,0	0,9	
E	4,4	3,8	9,6	2,9	1,2	

Q1

		V	W	X	Y	Z
A	<u>9</u> ,5	<u>8,7</u>		5,6	3,6	<u>9</u> ,2
B	2,5	7,6		3,5	<u>8</u> ,5	0, <u>8</u>
C	7,3	1,4		5,2	4,1	<u>9,7</u>
D	5,0	1,6		8, <u>9</u>	0,0	0, <u>9</u>
E	4,4	3,8		<u>9</u> ,6	2, <u>9</u>	1,2

Q2

	q	1-q
p	2,2	4,3
1-p	4,5	3,3

- Player 1:
 $2q + 4(1-q) = 4q + 3(1-q)$
Implies $q = 1/3$
- Player 2:
 $2p + 5(1-p) = 3$ implies $p = 2/3$

Q3

- Monopoly:

$$\pi_M = Q(100 - 0.5Q) - 20Q = 80Q - 0.5Q^2$$

$$\frac{\partial \pi_M}{\partial Q} = 0 \Rightarrow 80 - Q = 0 \Rightarrow Q = 80$$

$$P = 60$$

$$\pi_M = 3200$$

- Perfect competition:

$$P = 100 - 1/2Q = 20, \text{ thus } Q = 160 \text{ and zero profit.}$$

- Cournot:

$$\pi_1 = q_1 \times (100 - 0.5 \times (q_1 + q_2)) - 20q_1$$

$$= 80q_1 - \frac{1}{2}q_1^2 - \frac{1}{2}q_1q_2$$

$$\frac{\partial \pi_1}{\partial q_1} = 80 - q_1 - \frac{1}{2}q_2 = 0 \Rightarrow q_1 = 80 - \frac{1}{2}q_2$$

- $q_1 = q_2 = 53.3$

- $P = 46.6$

- $\Pi_1 = \Pi_2 = 1422$

- Cournot with unequal costs:

$$\pi_1 = q_1 \times (100 - 0.5 \times (q_1 + q_2)) - 10q_1$$

$$= 90q_1 - \frac{1}{2}q_1^2 - \frac{1}{2}q_1q_2$$

$$\frac{\partial \pi_1}{\partial q_1} = 90 - q_1 - \frac{1}{2}q_2 = 0 \Rightarrow q_1 = 90 - \frac{1}{2}q_2$$

$$- q_1 = 66.6; q_2 = 46.6$$

$$- P = 44.1$$

- Stackelberg:

$$\pi_1 = 80q_1 - \frac{1}{2}q_1^2 - \frac{1}{2}q_1q_2$$

$$= 80q_1 - \frac{1}{2}q_1^2 - \frac{1}{2}q_1(80 - \frac{1}{2}q_1) = 40q_1 - \frac{1}{4}q_1^2$$

$$\frac{\partial \pi_1}{\partial q_1} = 40 - \frac{1}{2}q_1 = 0 \Rightarrow q_1 = 80$$

- $q_1=80; q_2=40$

- $P=40$

- $\Pi_1=1600; \Pi_2=800$

Q4

- Table:

Candidate	Technical	Presentation	Motivation
A	1	0	0
B	0	1	0
C	1	1	0
D	0	0	1
E	0	1	1

Candidate	Technical	Motivation
C	1	0
E	0	1

Q5

incumbent

entrant		TV	Sales reps
	TV	1,9	3,7
	Sales reps	3,7	1,9

entrant		TV	Sales reps
	TV	-2,-2	-2,-1
	Sales reps	-1,-2	-1,-1

entrant		TV	Sales reps
	TV	-1, 7	1 ,6
	Sales reps	2 ,5	0, 8

- Mixed strategies

		TV p	Sales reps 1-p
TV	q	-1, 7	1 ,6
Sales reps	1-q	2 ,5	0, 8

- Entrant: $-1p + 1 - p = 2p$, $p = 1/4$
- Incumbent: $7q + 5(1 - q) = 6q + 8(1 - q)$, $q = 3/4$
- Entrant: $\pi = 0.5$
- Incumbent: $\pi = 6.5$

Q6

