#### **PROTEIN PHYSICS**

### **LECTURES 5-6**

Elementary interactions: hydrophobic & electrostatic; SS and coordinate bonds

#### **Hydrophobic effect**



Concentration of  $C_6H_{14}$  in  $H_2O$ : 50 times <u>less</u> than in gas!

WHY?

for ethanol:  $= \frac{1}{47000}$ 

#### <u>ENTROPY</u>:

 $S_E = k_B \cdot \ln[M_E];$   $M_E = number_of_states(E)$   $Why k_B? What is k_B?$ Because entropy  $S_E$  comes to the free energy  $F_E = E - TS_E$  (measured in energy units) as  $TS_E$ , and T is measured in degrees, while  $\ln[number of states]$  is dimensionless; Thus,  $k_B$  is energy\_unit/degree

FREE ENERGY:Probability(E) ~  $M_{E} \cdot exp(-E/k_{B}T) = exp(-F_{E}/k_{B}T)$ BoltzmannF=E-TS at V=const;G=H-TS=(E+PV)-TS at P=const (better for experiment)



G<sup>int</sup>: "Free energy of interactions" ("mean force potential")

Chemical potential:  $\mu \equiv G^{(1)} = G^{int} - T \cdot k_B ln(V^{(1)}) \equiv G^{int} + T \cdot k_B ln[C]$ EQUILIBRIUM for transition of molecule 1 from A to B:  $G_A^{(1)} = G_B^{(1)}$ chemical potentials in A and B are equal

$$\Delta G^{int}_{A \to B} \equiv G^{int}_{B} - G^{int}_{A}$$
$$\Delta G^{int}_{A \to B} = k_{B} T \cdot \ln([C_{inA}]/[C_{inB}])$$



# Experiment: $\Delta G_{A \to B}^{int} = k_B T \cdot \ln([C_{1inA}]/[C_{1in}])$



[C] of C<sub>6</sub>H<sub>12</sub> in  $H_2O$ : 50 times less than in gas; 100000 times less than in liquid C<sub>6</sub>H<sub>12</sub>



#### **H-bond: directed**





0.5.0.51

TI CO



#### "hydrophobic bond"



High heat capacity d(ΔH)/dT: Melting of "iceberg"







20-25 cal/mol per Å<sup>2</sup> of molecular accessible non-polar surface





Hydrophobic effect & denaturation of proteins



WALTER KAUZMANN

1916-2009

Cyrus Homi **Chothia**, 1942

> Hydrophobic effect & amino acid water-accessible surface

Семён Ефимович **Бреслер** Давид Львович **Талмуд** (1911 – 1983) (1900 - 1973) Hypothesis on a role of hydrophobic effect in protein folding



Charles **Tanford** (1921 - 2009)

General physical features of Hydrophobic effect





Electrostatics in uniform media: potential  $\phi_1 = q_1/\epsilon r$ Interaction of two charges:  $U = \phi_1 q_2 = \phi_2 q_1 = q_1 q_2 / \epsilon r$  $\epsilon = 1$  vacuum  $\epsilon \approx 3$  protein ε ≈ 80 water **Protein/water interface** In non-uniform media:  $\epsilon_{eff} = ?$  $\mathcal{E}_{eff} = ?$ At atomic distances:

#### Charles-Augustin de Coulomb



(1736-1806)



 $\Delta U_{1 \Rightarrow 2} = q^2/2\varepsilon_2 R - q^2/2\varepsilon_1 R$ 

Water => vacuum:  $\Delta U \approx +100$ Kcal/mol R=(1.5-2 Å) +0.1Å R=(1-1.5 Å) +0.7Å R=(0.5-1 Å) +0.7Å



Water => PROTEIN ( $\epsilon \approx 3$ )  $R \approx 1.5 - 2 \text{ Å}$  $\Delta U \approx +30 - 40 \text{ kcal/mol}$ 

CHARGE inside PROTEIN: VERY BAD



## Non-uniform media:

#### KNOWN: molecules (dipoles) decrease potential: U ~ 1/εr

Eeff







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 $\begin{array}{c} \bigotimes & \stackrel{+}{\oplus} & \bigotimes \\ \bigoplus & \bigoplus & \vdots \end{array} \\ \bigoplus & \bigoplus & \vdots \end{array} \\ & \bigoplus & \varepsilon_1 \approx 80 \end{array}$ (T)



Good estimate for non-uniform media

ε<sub>eff</sub> ≈ 150 !!





effective in nonuniform media



### Atomic distance:

 $\varepsilon_{eff} = ?$ 

intermediate "vacuum", ε~1? but the absence

of intermediate dipoles can only increase interaction...



At atomic distances in water:

1)  $\varepsilon$ =80 is not a bad approximation (much better than  $\varepsilon$  = 1 or 3 !!) (salt does not dissolve, if  $\varepsilon$ <50 at 3Å!)



ΔG<sub>el</sub> = 2.5 × In(10) × RT ≈ 6RT ≈ 3.5 kcal/mol at ≈2.5Å ε ≈ 30-40 at ≈ 2.5Å!



Protein engineering experiments:  $\phi(\mathbf{r}) = \Delta \mathbf{p} \mathbf{H} \times 2.3 \mathbf{RT} \Rightarrow \boldsymbol{\epsilon}_{eff}(\mathbf{r})$ 







Sir Alan Roy Fersht, 1943

Protein engineering

## <u>Dipole</u> interactions (e.g., H-bonds):



#### **Quadruple** interactions



quadruple ~ 1/ɛr<sup>3</sup>

#### (HO)<sup>-1/3</sup>-H<sup>+1/3</sup>:::::(OH)<sup>-1/3</sup>-H<sup>+1/3</sup>

Also: charge-dipole, dipole-quadruple, etc.

Potentials:

$$\phi_{dipole} \sim 1/\epsilon r^2$$

Electrostatic interactions also occur between charge (q) and non-charged body, if its  $\epsilon_2$  differs from the media's  $\epsilon_1$ :

$$\bigcup \sim \mathbf{q} \cdot \left[\frac{1}{\epsilon_2} - \frac{1}{\epsilon_1}\right] \cdot \left[\frac{\epsilon_2}{2} / (\frac{\epsilon_1 + \epsilon_2}{2} / 2)\right] \cdot \bigvee \cdot (1/\Gamma^4) \quad \text{at large } \Gamma$$

In water: repulsion of charges from non-polar molecules (since here  $\epsilon_1 >> \epsilon_2$ ); in vacuum (where  $\epsilon_1 < \epsilon_2$ ): just the opposite!



Debye-Hückel screening of electrostatic by ions:

 $U = [q_1 q_2 / \varepsilon r] \cdot exp(-r/D);$ 

in water:  $D = 3Å \cdot I^{-1/2}$ ;

Ionic strength  $I = \frac{1}{2}\sum_{i}C_{i}(Z_{i}^{\text{ion}})^{2}$ .

Usually:  $I \approx 0.1$  [mol/liter];  $D \approx 8$ Å.

Electrostatics is an example of a multi-body (charge1, charge2, media, ions) interaction

**Electrostatics is T-dependent;**  $U = (1/\epsilon) \cdot (q_1 q_2/r)$ is free energy (U = H-TS);  $TS = T \cdot (-dU/dT) = -T \cdot [d(1/\epsilon)/dT] \cdot (q_1 q_2/r) =$ =  $[dln(\epsilon)/dlnT] \cdot U$ in water: when T grows from 273° to 293°K (by 7%), E decreases from 88 to 80 (by 10%): -TS ≈ 1.3U; H ≈ -0.3U In water the entropic term (-TS) is the main for electrostatics!

## S-S bonds (Cys-Cys)

PROT	EIN +	GS-SG	$\leftrightarrow$	PROT	EIN +	GSH	$\leftrightarrow$	PROTEIN +	2GSH
1	1			1	1			$\lambda$ /	
SH	HS			SH	S-SG			S-S	

## exchange:

entropic force

S-S bond is not stable within a cell

## Coordinate bonds (with Zn<sup>++</sup>, Fe<sup>+++</sup>,...)





exchange:

entropic

force