Principles of Macroeconomics

ECO 1019 Lecture 5
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## In this Lecture:

- Consumer's consumption/savings decision - responses of consumer to changes in income and interest rates.
- Government budget deficits and the Ricardian Equivalence Theorem.


## Intertemporal decisions

- They involve a trade off across periods of time: between current and future consumption, between current and future taxes, etc.
- In Solow model: arbitrary intertemporal decision rule, constant saving rate
- We use microeconomic principles to have a more detailed analysis


## Our model

- Two period model: today and tomorrow
- For simplicity: income is exogenous (no work/leisure decision). This helps us focus on the consumption-savings decision
- Lump sum taxes


## Budget Constraints

The consumer's current-period budget constraint:

$$
c+s=y-t \left\lvert\, \begin{aligned}
& \text { We assume a credit } \\
& \text { market in which we } \\
& \text { trade a bond issued } \\
& \text { either by the consumers } \\
& \text { or the government }
\end{aligned}\right.
$$

$s>0$ : consumer is a lender on the credit market
$s<0$ : consumer is a borrower on the credit market

## Budget Constraints

The consumer's future-period budget constraint:

$$
c^{\prime}=y^{\prime}-t^{\prime}+(1+r) s
$$

## Simplify

Solve the future-period budget constraint for s:

$$
s=\frac{c^{\prime}-y^{\prime}+t^{\prime}}{1+r}
$$

## Next,

Substitute in the current-period budget constraint obtaining lifetime budget constraint:

$$
c+\frac{c^{\prime}-y^{\prime}+t^{\prime}}{1+r}=y-t
$$

## Consumer's Lifetime Budget Constraint

Substitute in the current-period budget constraint obtaining lifetime budget constraint:


## Simplified Lifetime Budget Constraint

$$
c+\frac{c^{\prime}}{1+r}=w e
$$

## Simplified Lifetime Budget Constraint: Slope-Intercept

$$
c^{\prime}=-(1+r) c+w e(1+r)
$$

## Consumer's Lifetime Budget Constraint



## A Consumer's Indifference Curves



## Sara's Desire for Consumption Smoothing

| Table 8.1 | Sara's Desire for Consumption Smoothing |  |  |
| :--- | :---: | :---: | :---: |
|  | Week 1 <br> Coconuts | Week 2 <br> Coconuts | Total <br> Consumption |
| Bundle 1 | 5 | 15 | 20 |
| Bundle 2 | 17 | 3 | 20 |
| Preferred Bundle | 11 | 9 | 20 |

## Optimization

Marginal condition that holds when the consumer is optimizing:

$$
M R S_{c, c^{\prime}}=1+r
$$

## A Consumer Who Is a Lender



## A Consumer Who Is a Borrower



## An Increase in Current Income for the Consumer

- Current and future consumption increase.
- Saving increases.
- The consumer acts to smooth consumption over time.


## The Effects of an Increase in Current Income for a Lender



## Observed Consumption-Smoothing Behavior

- If all consumers try to smooth consumption overtime, we should observe that aggregate consumption is smoother than aggregate income
- Aggregate consumption of non-durables and services is smooth relative to aggregate income, but the consumption of durables is more volatile than income.
- This is because durables consumption is economically more like investment than consumption.


## Percentage Deviations from Trend in Consumption of Durables and Real GDP



Percentage Deviations from Trend in Consumption of Nondurables and Services and Real GDP


## An Increase in Future Income for the Consumer

- Current and future consumption increase.
- Saving decreases.
- The consumer acts to smooth consumption over time.


## An Increase in Future Income



## Temporary and Permanent Increases in Income

- As a permanent increase in income will have a larger effect on lifetime wealth than a temporary increase, there will be a larger effect on current consumption.
- A consumer will tend to save most of a purely temporary income increase.
- This is the permanent income hypothesis by Milton Friedman


## Temporary Versus Permanent Increases in Income



## An Increase in the Real Interest Rate



## An Increase in the Market Real Interest Rate

An increase in the market real interest rate decreases the relative price of future consumption goods in terms of current consumption goods - this has income and substitution effects for the consumer.

## An Increase in the Real Interest Rate for a Lender



## Effects of an Increase in the Real Interest Rate for a Lender

Table 8.2 Effects of an Increase in the Real Interest Rate for a Lender

Current consumption
Future consumption
Current savings
Increases
?

## An Increase in the Real Interest Rate for a Borrower



## Effects of an Increase in the Real Interest Rate for a Borrower

Table 8.3 Effects of an Increase in the Real Interest Rate for a Borrower

Current consumption
Future consumption
Current savings

Decreases
?
Increases

## Introducing the government

- Government buys $G$, financed either with taxes or debt.
- $T=N t, T^{\prime}=N t^{\prime}$
- Private and government bonds are indistinguishable, have same interest rate $r$


## Government Budget Constraints

The government's current-period budget constraint:

$$
G=T+B
$$

## Government Budget Constraints

The government's future-period budget constraint:

$$
G^{\prime}+(1+r) B=T^{\prime}
$$

## Government Budget Constraints

The government's present-value budget constraint:

$$
G+\frac{G^{\prime}}{1+r}=T+\frac{T^{\prime}}{1+r}
$$

## Competitive equilibrium

- Each consumer chooses current and future consumption and savings optimally given interest rate $r$
- The government present-value budget constraint holds
- The credit market clears


## Credit Market Equilibrium Condition

Total private savings is equal to the quantity of government bonds issued in the current period.

$$
S^{p}=B
$$

## Credit Market Equilibrium: Implications

Remember: $\quad S=S^{p}+S^{g}=I+C A$
Here $I=O, C A=O$, and $S^{g}=-B$

$$
\begin{gathered}
S^{p}=Y-C-T \\
B=G-T
\end{gathered}
$$

Therefore,

$$
S^{p}=B \Leftrightarrow Y-C-T=G-T
$$

Or rearranging

$$
Y=C+G
$$

## Income-Expenditure Identity

Credit market equilibrium implies that the income-expenditure identity holds.

$$
Y=C+G
$$

## Ricardian Equivalence

- The Ricardian Equivalence Theorem states that, under some conditions, a change in the timing of taxes is neutral, i.e. has no effect on the interest rate and on current and future consumption


## Ricardian Equivalence

Key equation: The consumer's lifetime tax burden is equal to the consumer's share of the present value of government spending - the timing of taxation does not matter for the consumer.

$$
N t+\frac{N t^{\prime}}{1+r}=G+\frac{G^{\prime}}{1+r}
$$

implies

$$
t+\frac{t^{\prime}}{1+r}=\frac{1}{N}\left(G+\frac{G^{\prime}}{1+r}\right)
$$

## Ricardian Equivalence

Then, substitute in the consumer's budget constraint taxes do not matter in equilibrium for the consumer's lifetime wealth, just the present value of government spending.

$$
c+\frac{c^{\prime}}{1+r}=y+\frac{y^{\prime}}{1+r}-\frac{1}{N}\left[G+\frac{G^{\prime}}{1+r}\right]
$$

## Ricardian Equivalence with a Cut in Current Taxes for a Borrower



## Ricardian Equivalence and Credit Market Equilibrium



## Discussion of the assumptions

- Ricardian equivalence theorems says government debt represents our future liabilities as a nation, must be paid by taxing citizens in the future.
- It's a good benchmark to start thinking about government debt, however some of the assumptions are very strong!
- Situations in which it might not hold:
- Heterogeneity: different taxes for different people
- Finite lifetimes
- Distortionary taxes
- Imperfections in the credit markets


## Readings

- Savings are generally a good idea http://www.youtube.com/watch?v=C 8TGTKdrlY
- The cost of repair http://www.economist.com/node/17173933?story id=17173 933
- Economists show "Cash-for-clunkers" was a clunker http://www.theatlantic.com/business/archive/2010/10/econ omists-show-cash-for-clunkers-was-a-clunker/65356/

